

Exploiting Task-Order Information in Optimizing Compilers for Parallel Programs

Christoph Angerer

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- Parallel programming becomes increasingly mainstream
- Influences **models, languages, runtime libraries**
- Added support for:
 - Controlling access to **shared data**
 - Controlling parallel **program flow**

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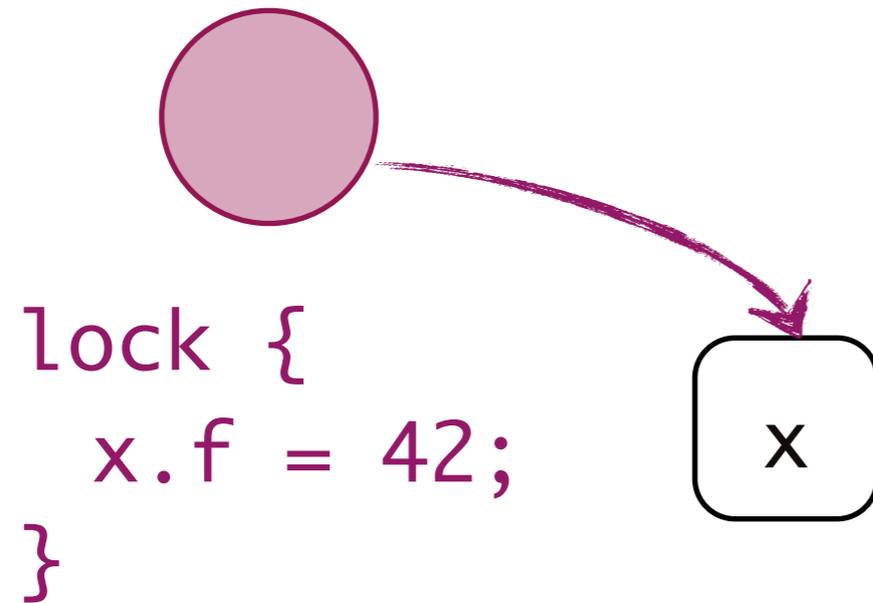
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Can a compiler exploit information about the execution-order of tasks?

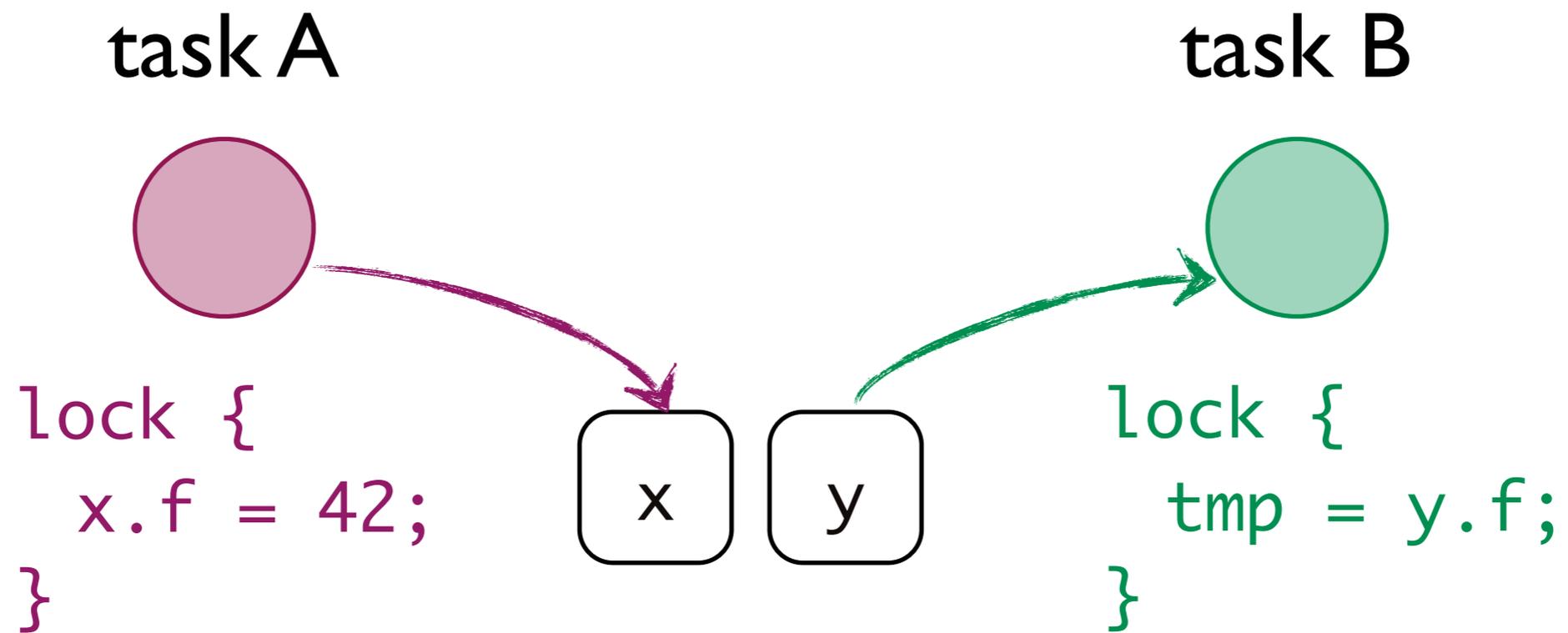
Example

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task A

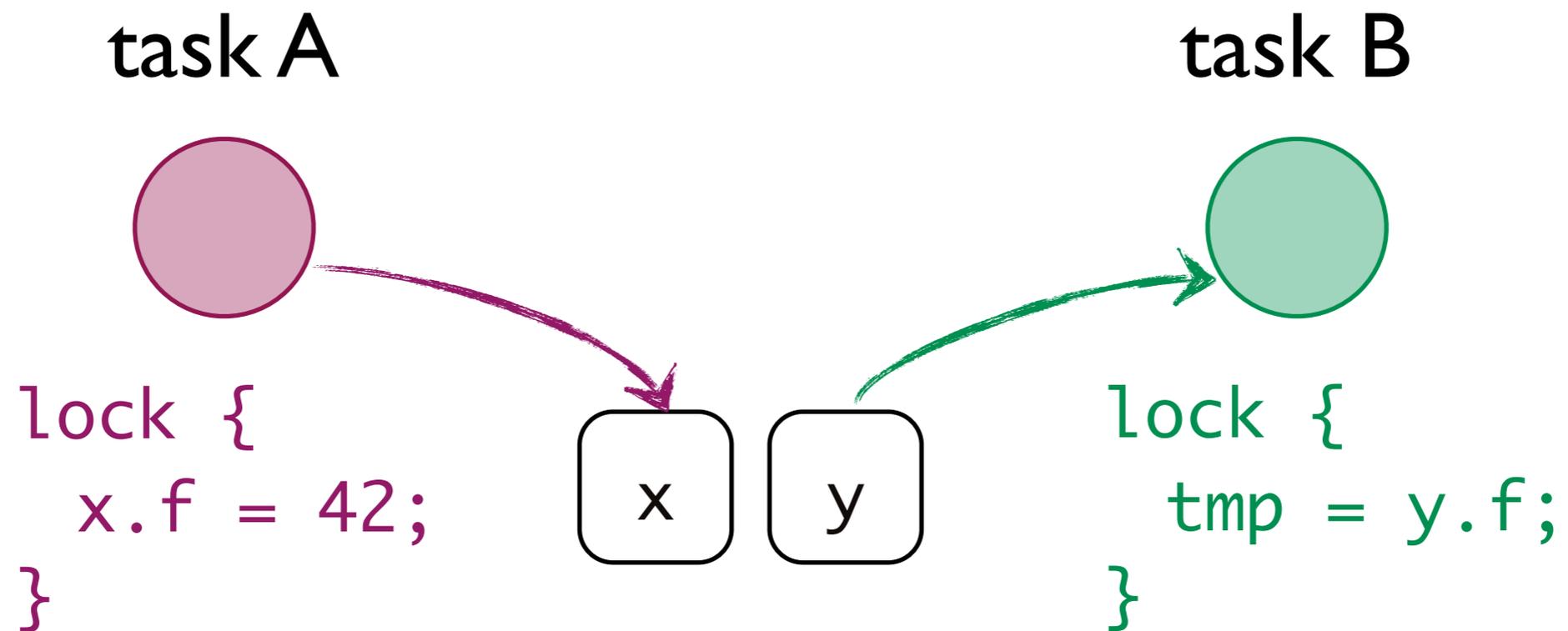


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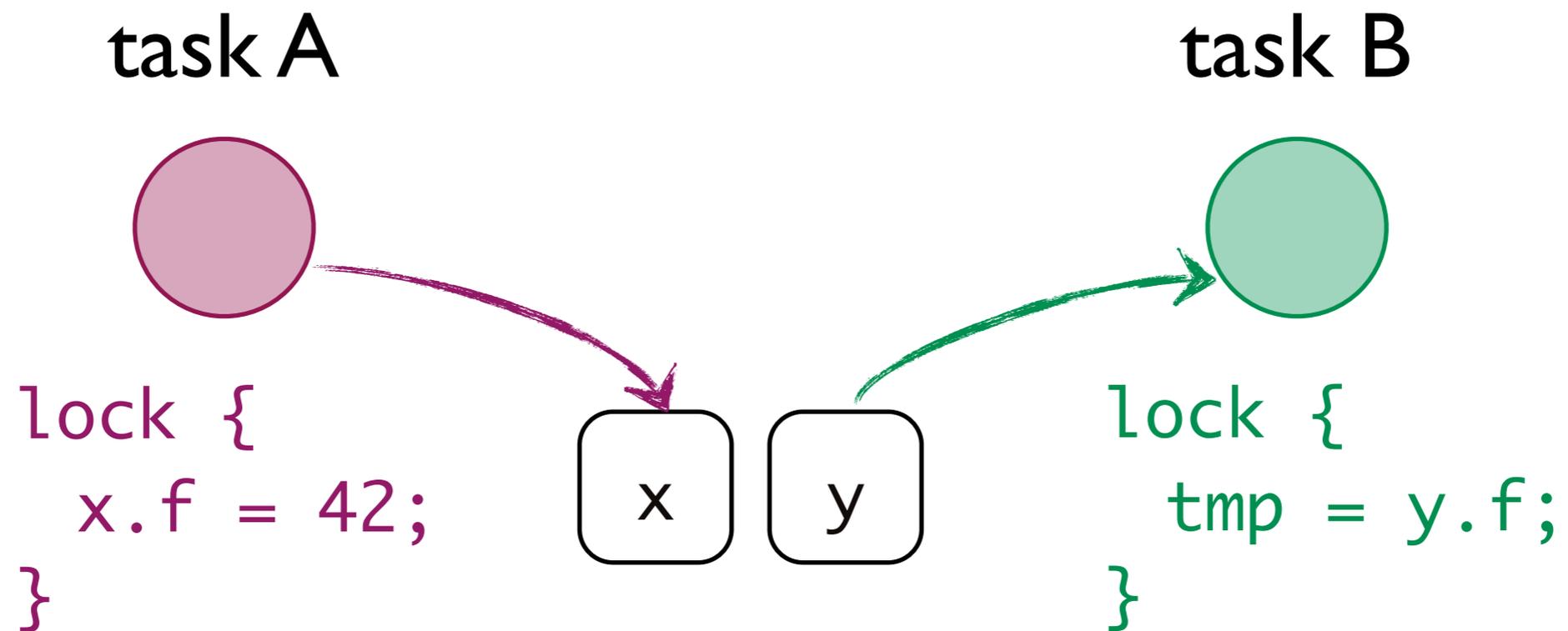
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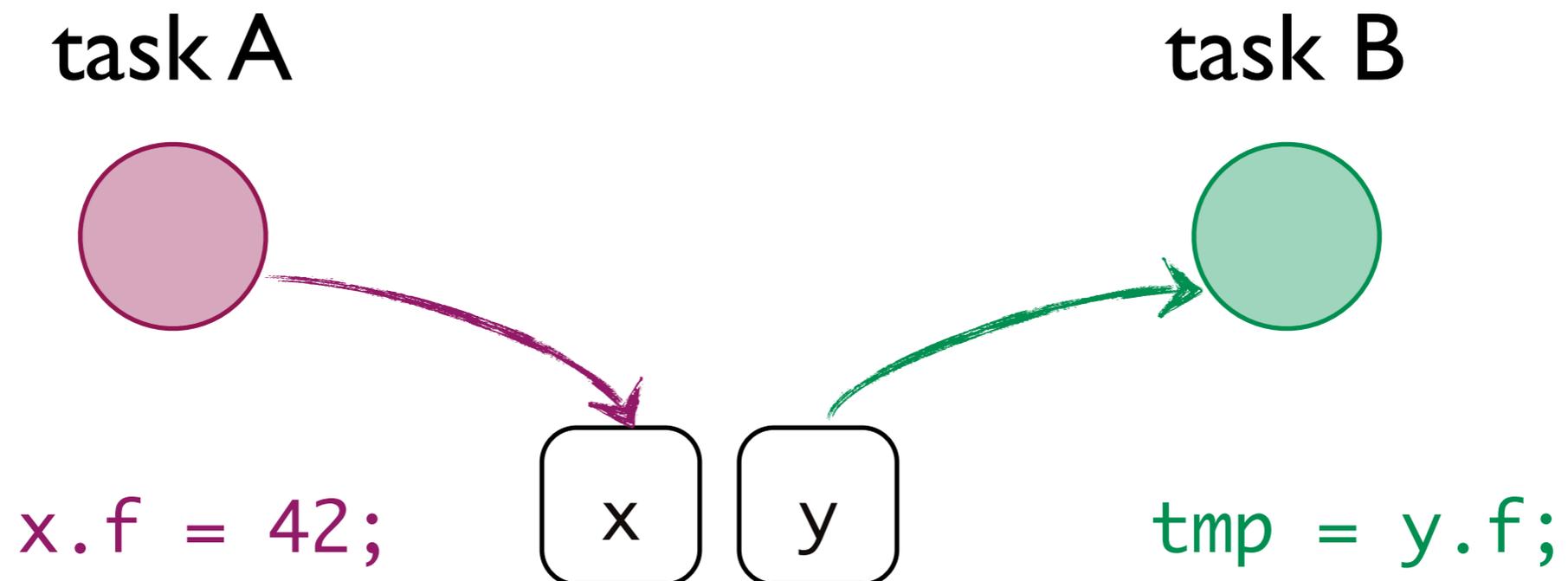
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Different Objects

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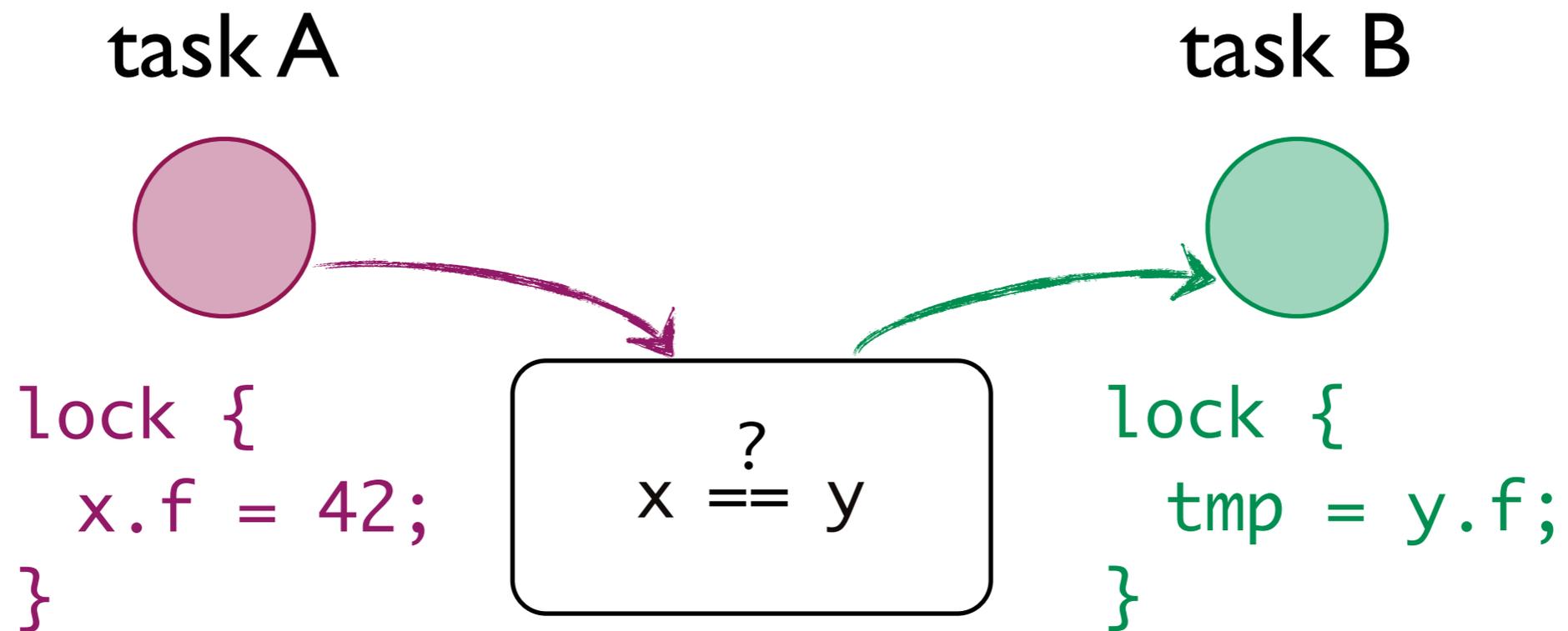
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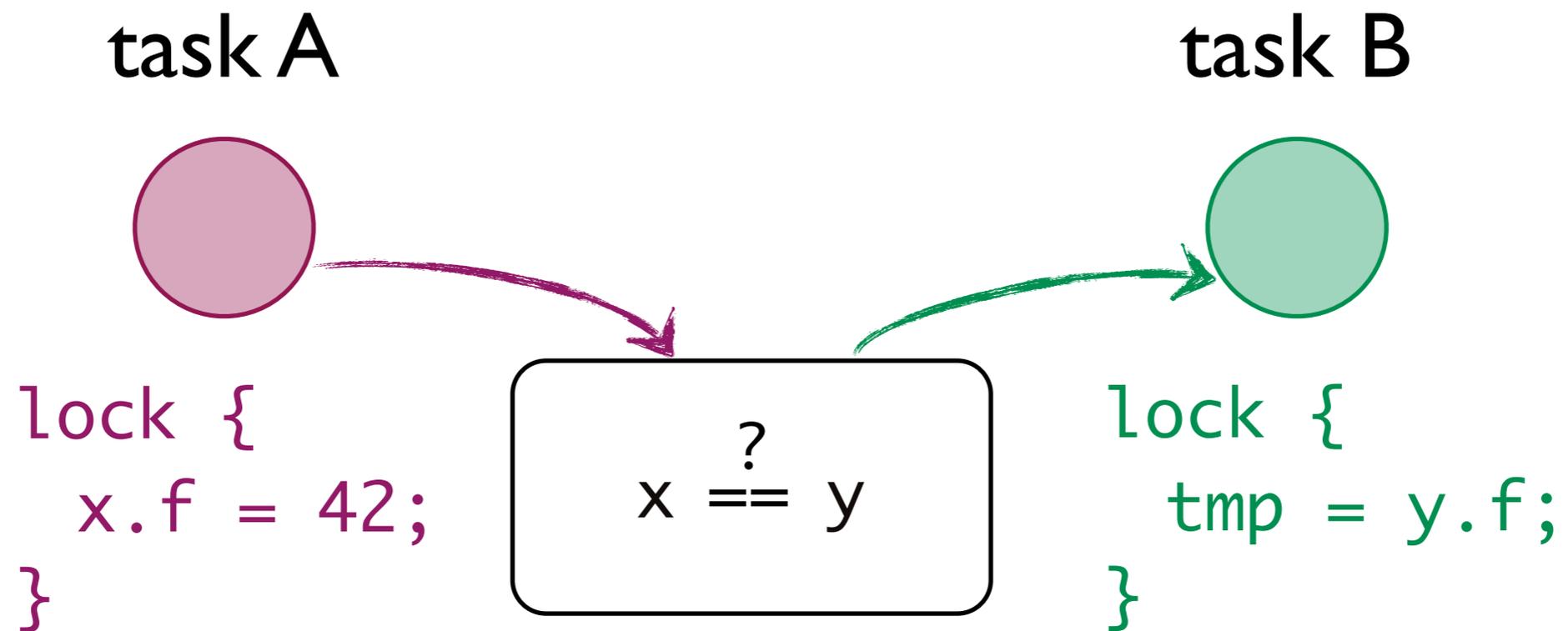
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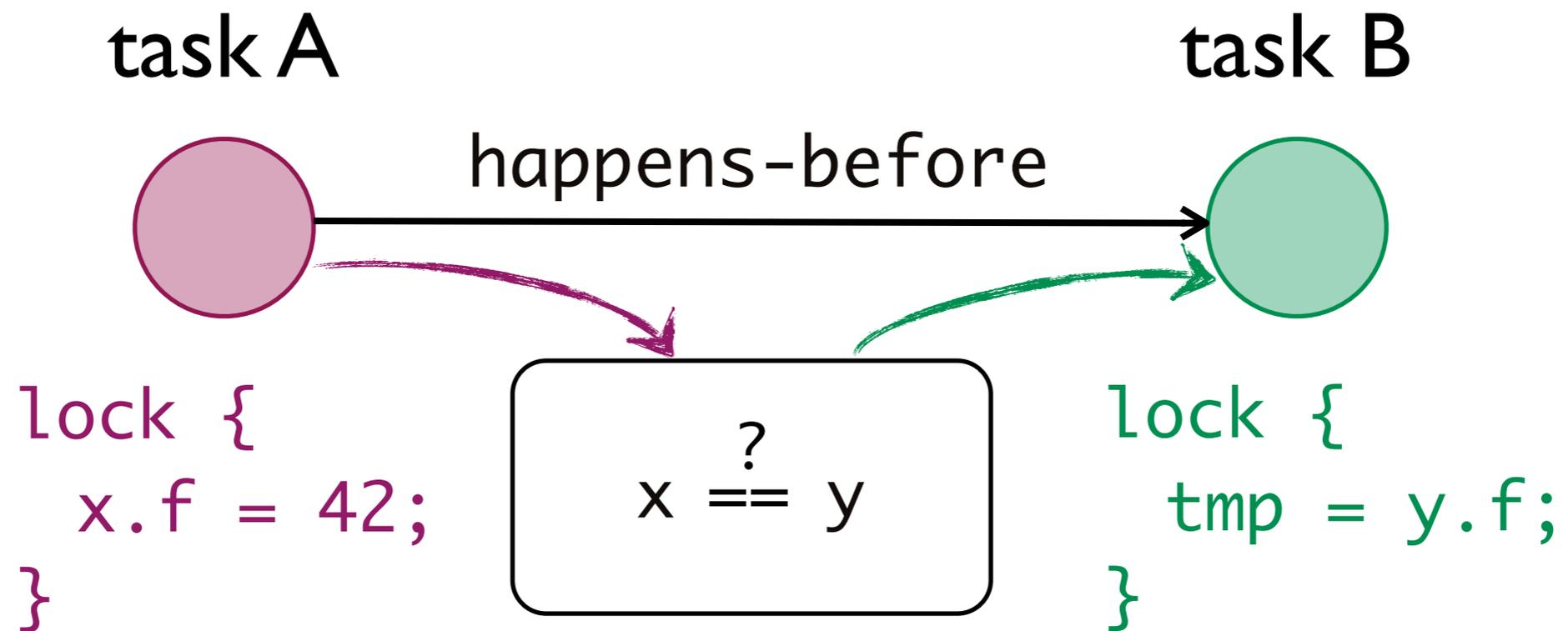
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Potentially aliased

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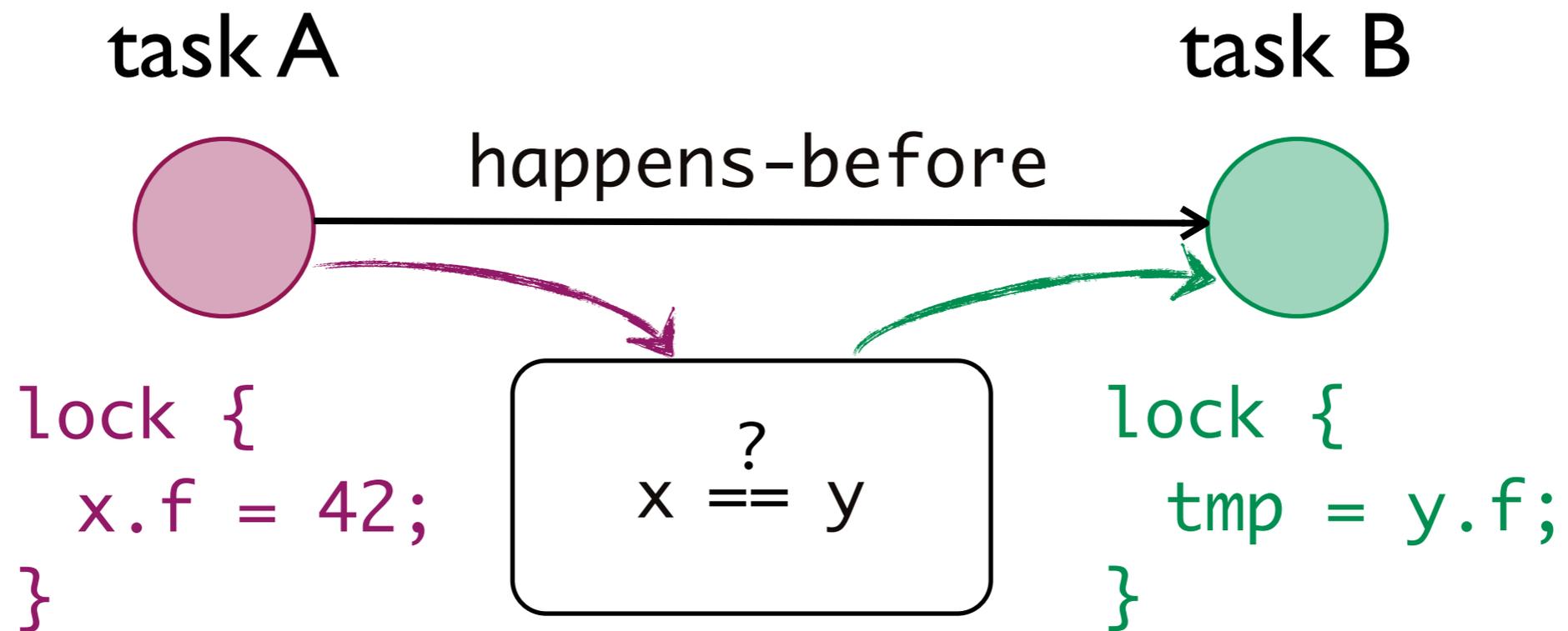
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Potentially aliased

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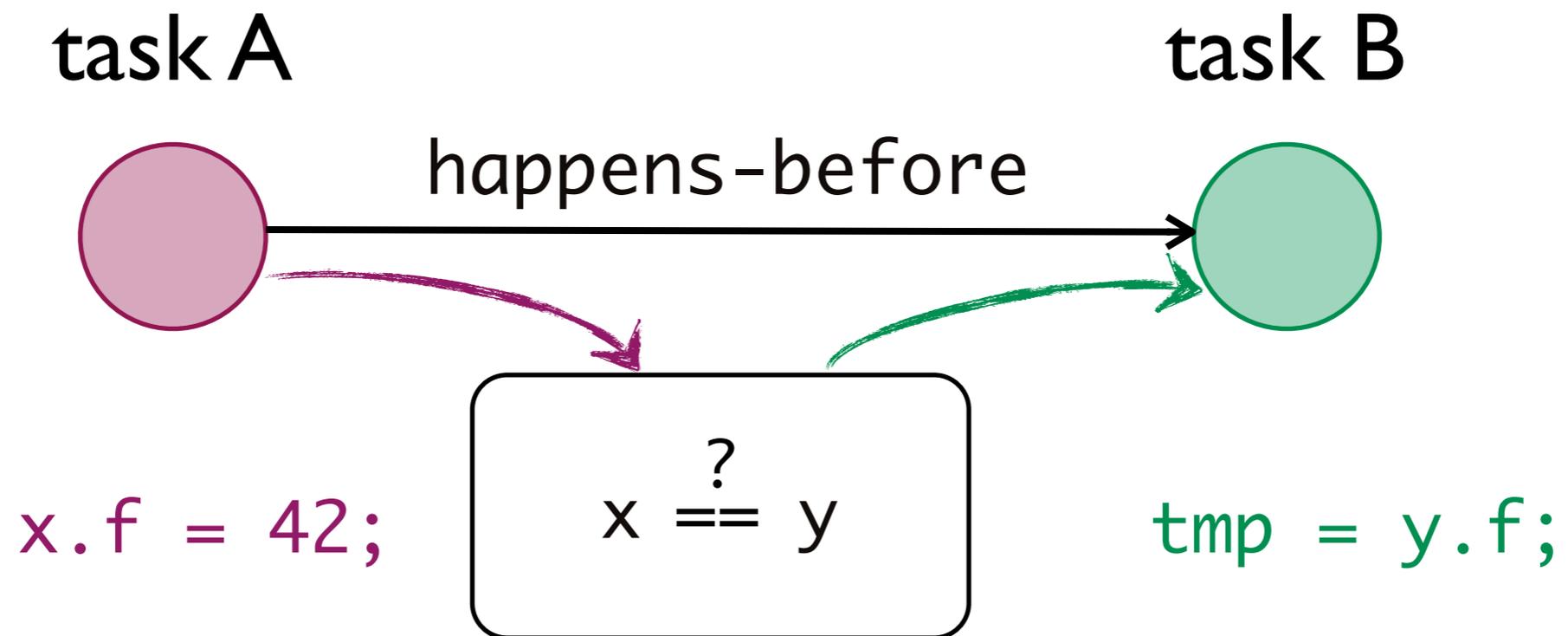


Potentially aliased

Ordered memory access

Example

- Can the compiler remove the lock?



Potentially aliased

Ordered memory access

Thesis Statement

“Effective optimizations for shared-memory parallel programs need task-order information.”

Contributions

- **Programming model** with explicit task-ordering constraints
- **Schedule analysis** to extract task-order information
- Evaluation of **compiler optimizations** that use task-order information

Outline

- Motivation
- **Task Model**
- **Schedule Analysis**
- **Two Case Studies**
- **Conclusion**

Sources of Task-Ordering

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- **Threads (Java)**
 - **Low-level signalling, difficult to analyze** [Barik 2006]

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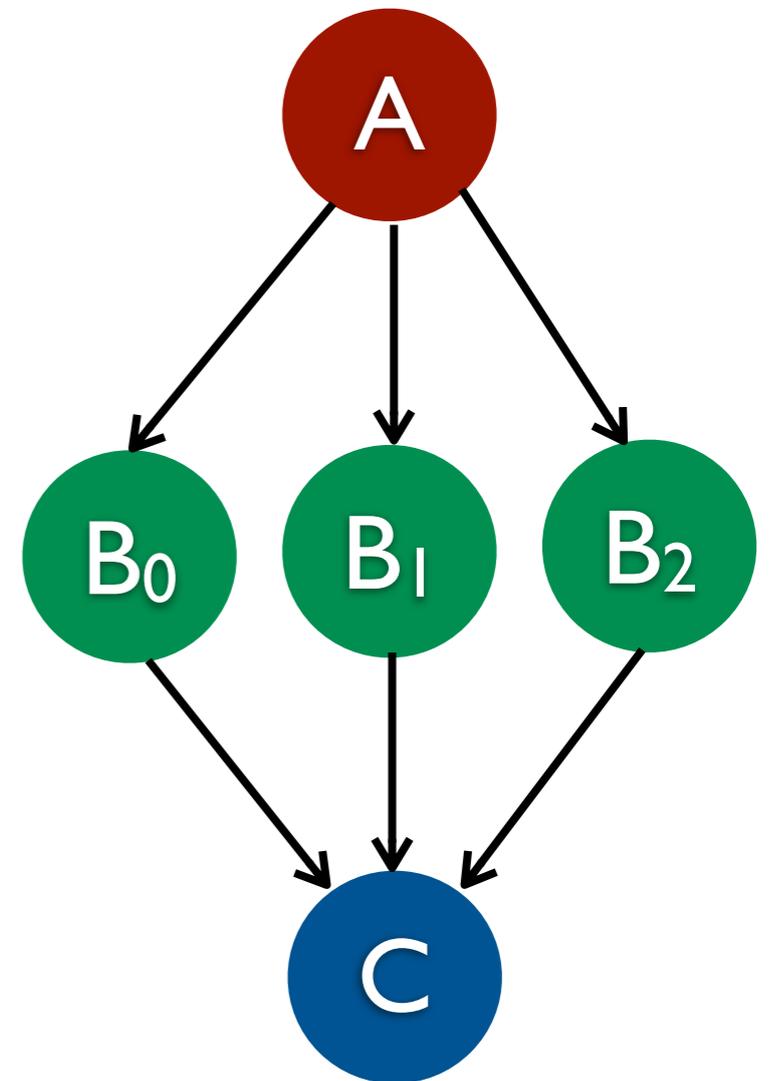
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- **Fork/join (OpenMP, X10, Cilk)**
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- **Task Libraries (Apple GCD, Microsoft TPL, Intel TBB)**
 - **Feature explicit task ordering**
 - **Not much previous work here**

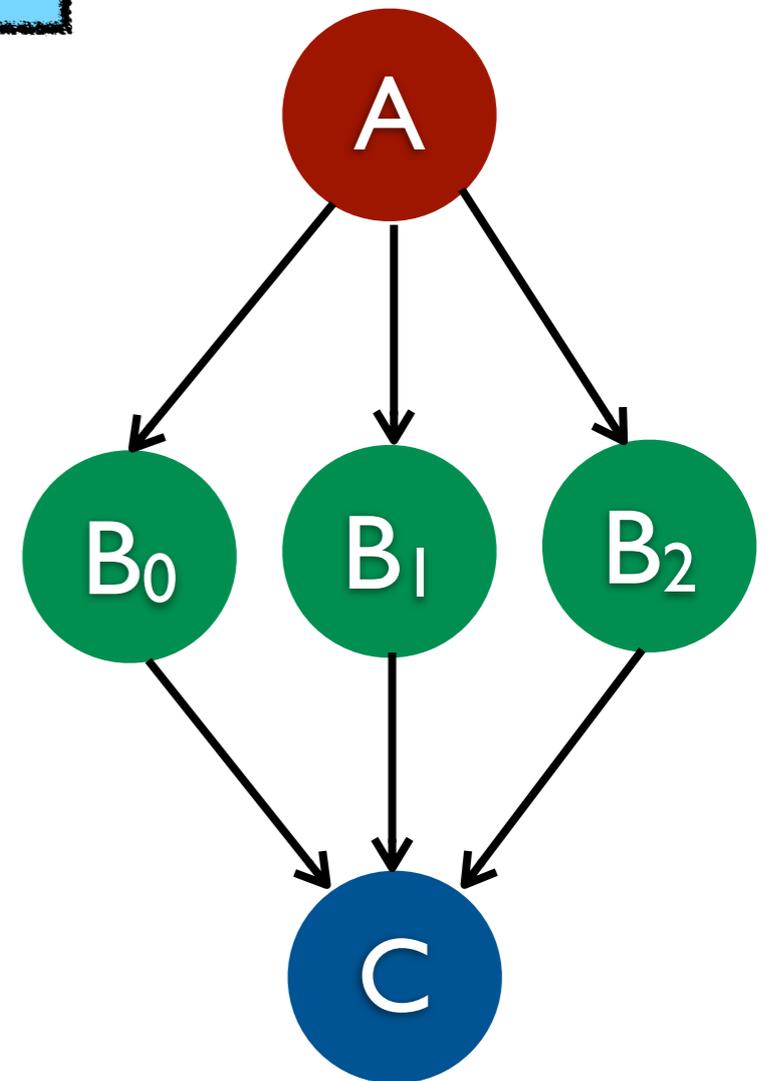
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```
Task tA = Task.StartNew(/*A*/);  
  
for(int i=0; i<3; i++) {  
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```



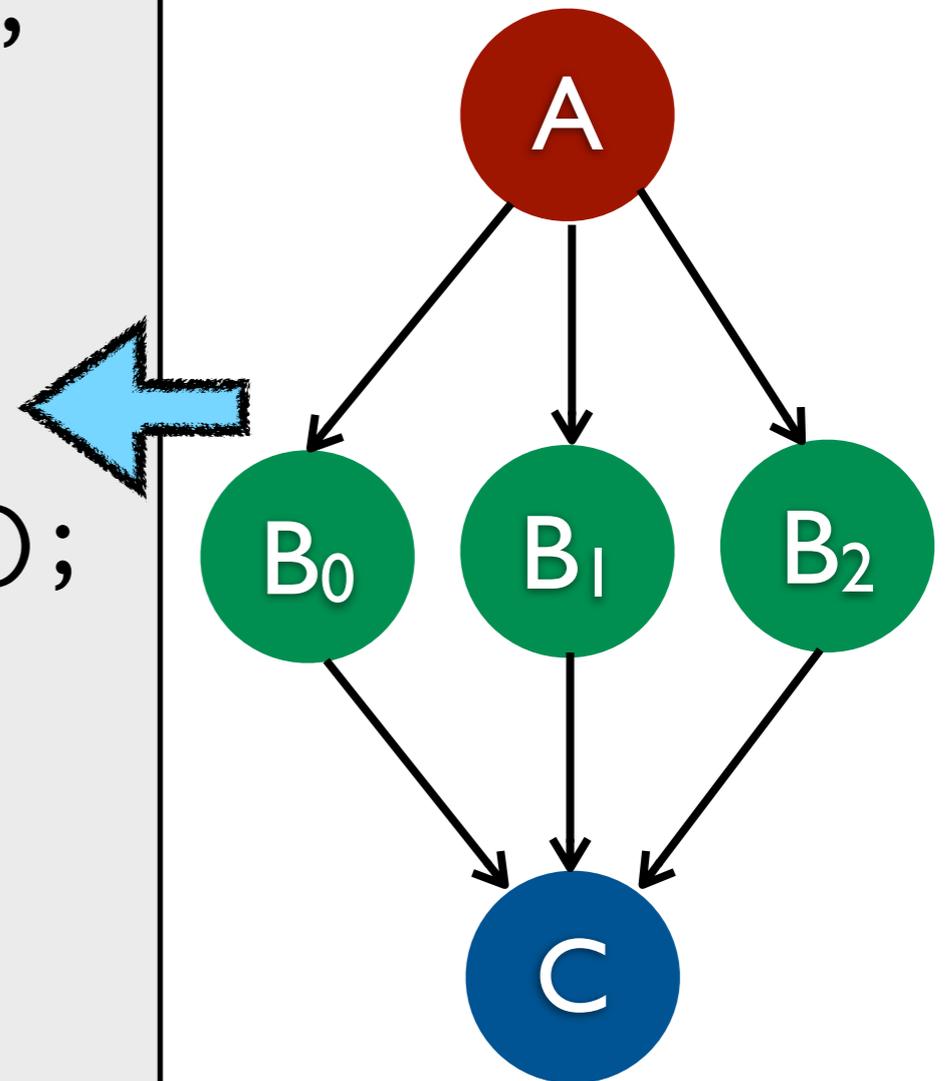
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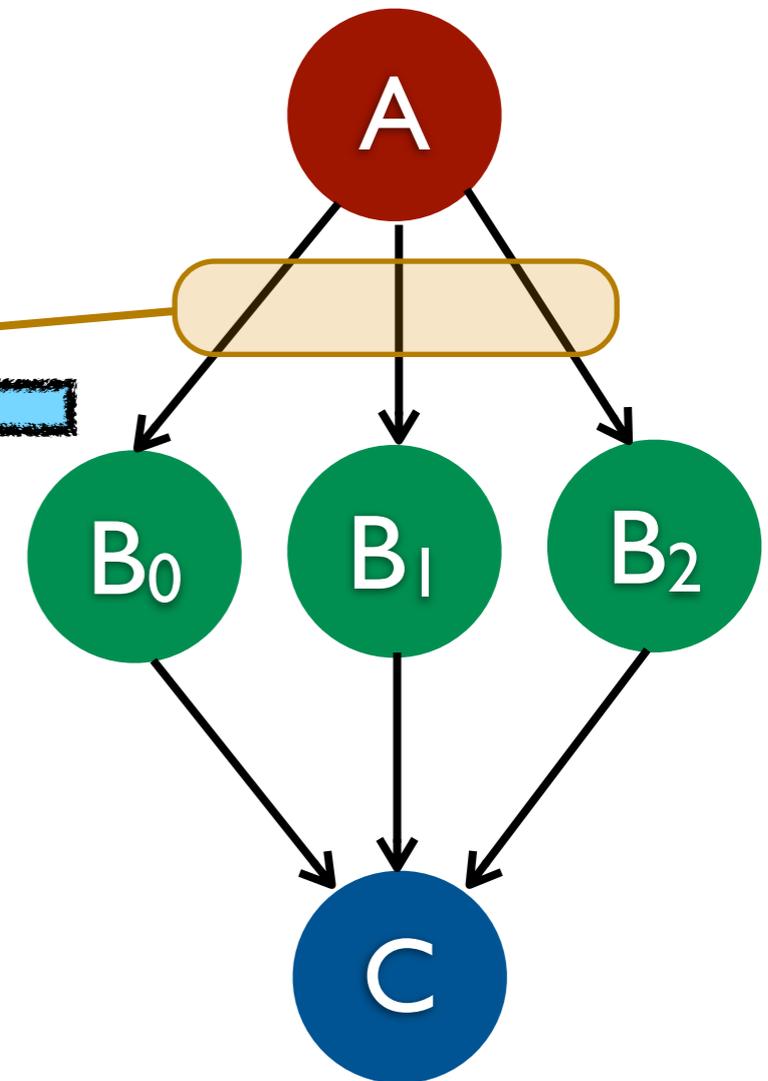
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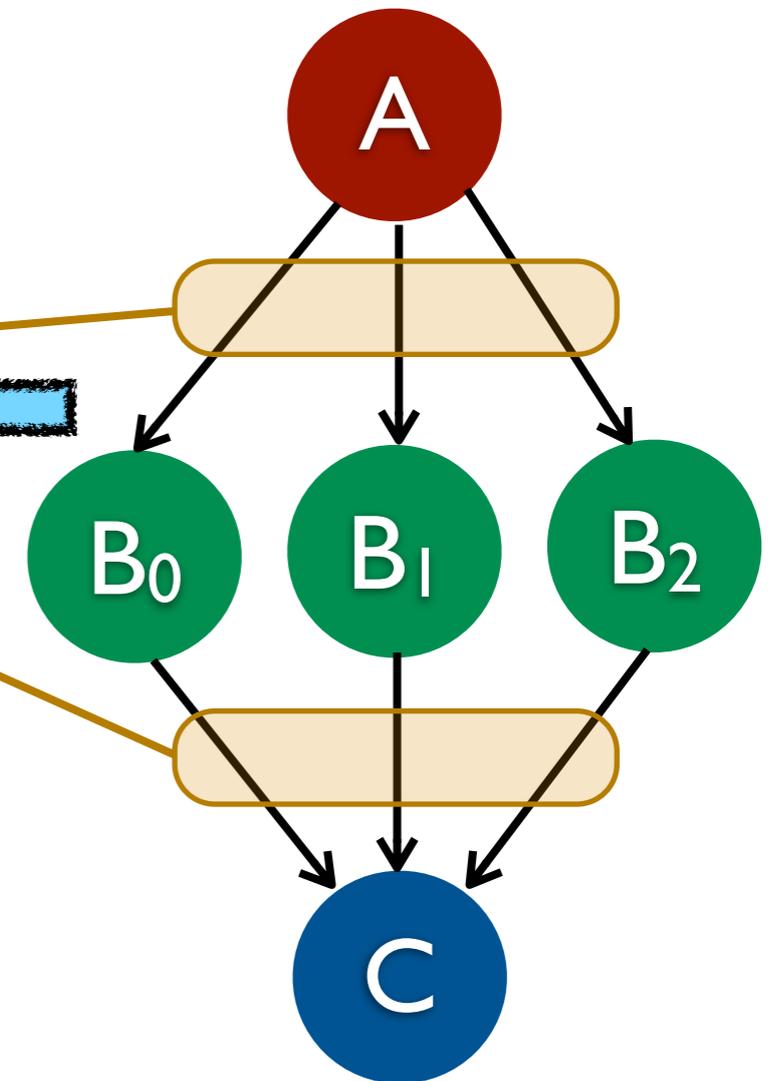
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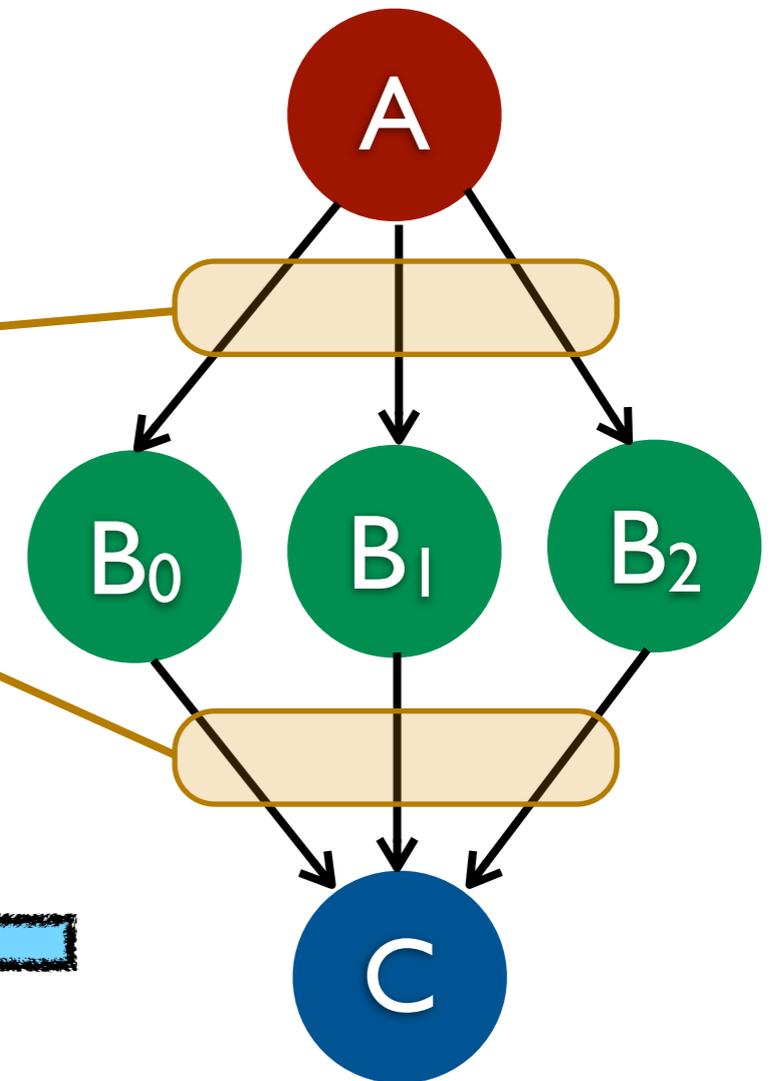
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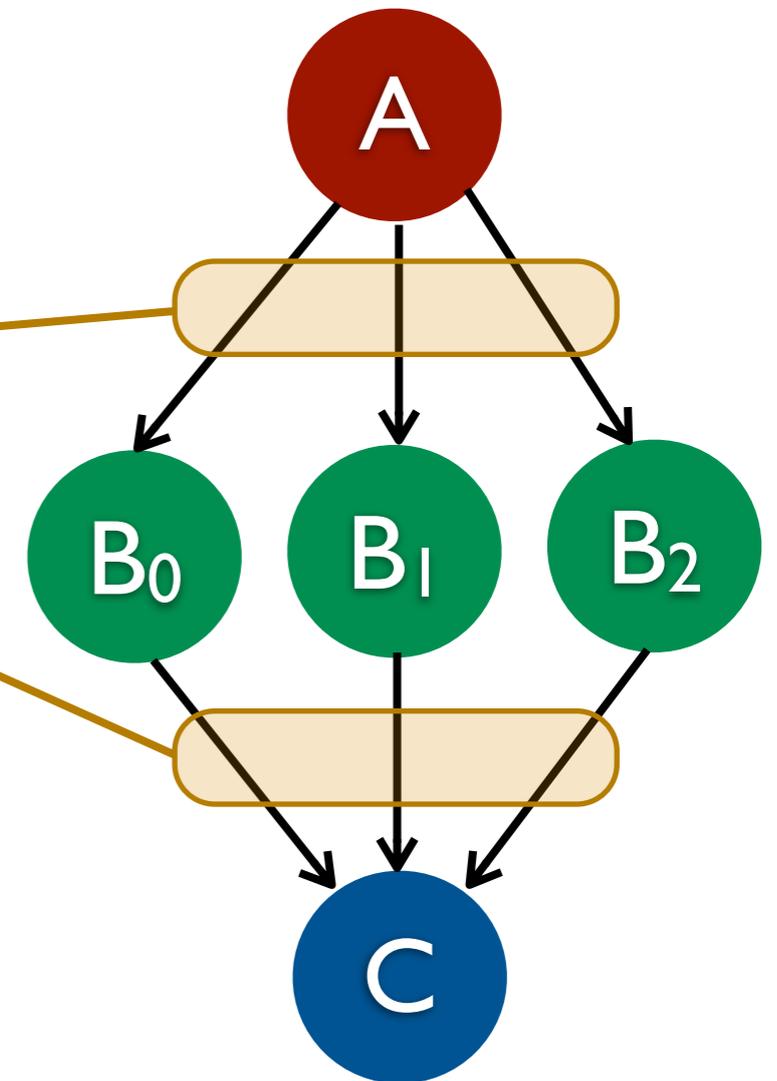
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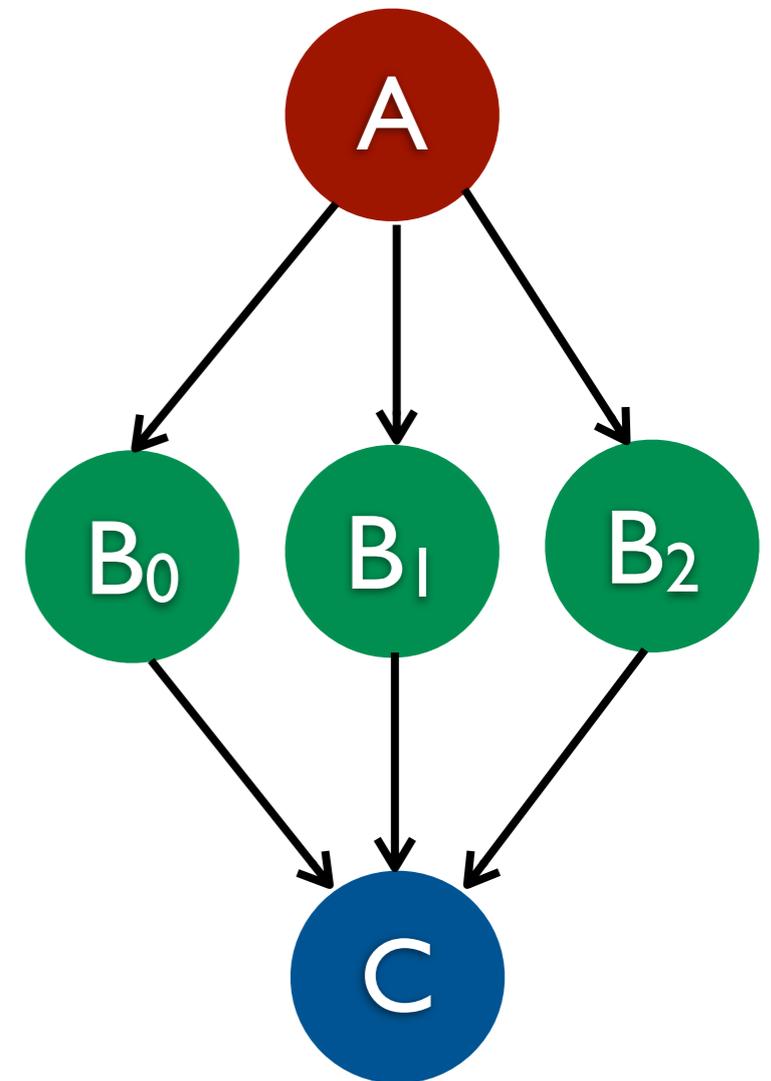
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 - Low-level, hard to analyze
- Fork/join
 - Lexical
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Abstraction:

**Tasks with explicit
happens-before
relationships**

Our Model: Explicit Scheduling

```
Task a = schedule /*A*/;  
Task c = schedule /*C*/;  
  
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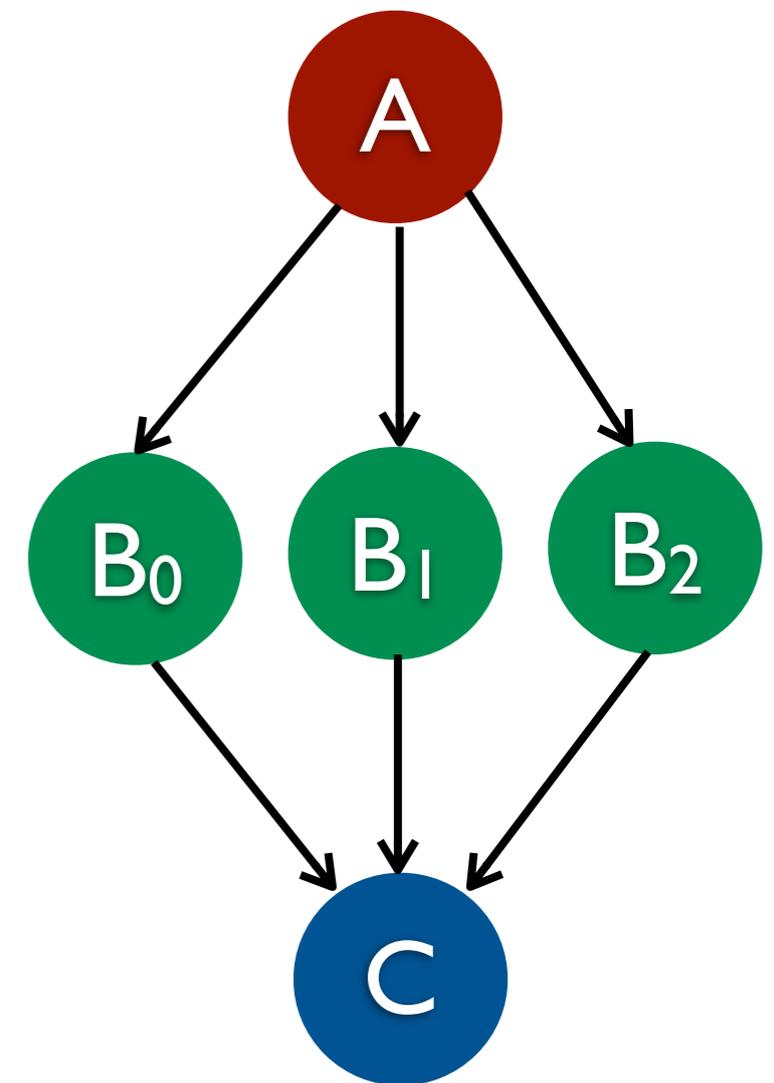
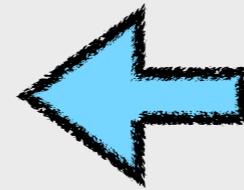


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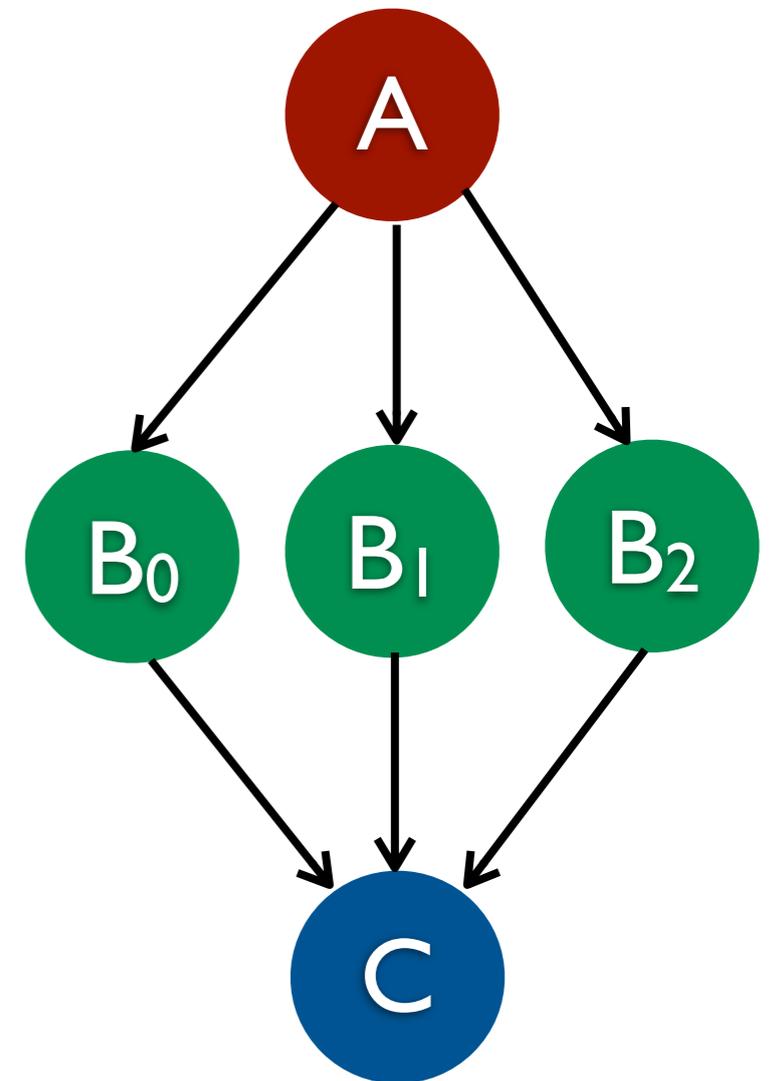
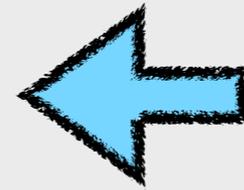
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Task c = schedule /*C*/;
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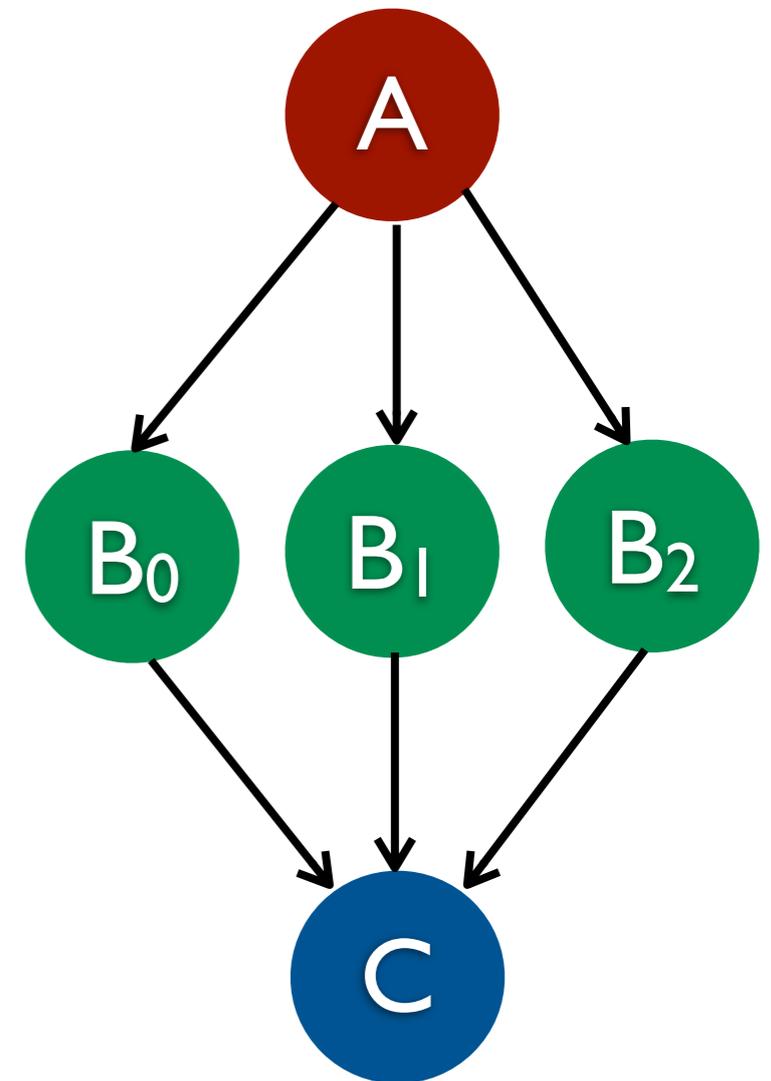
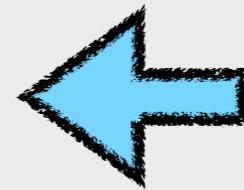
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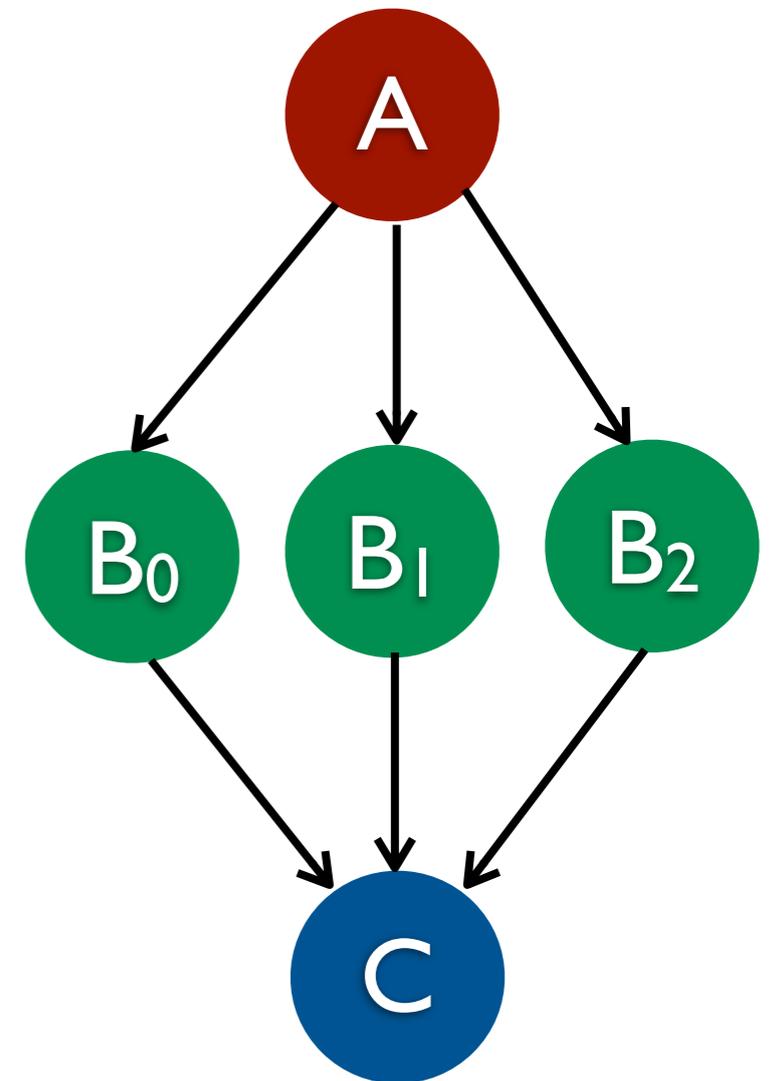
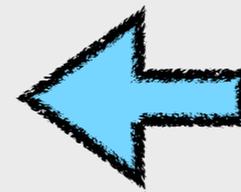
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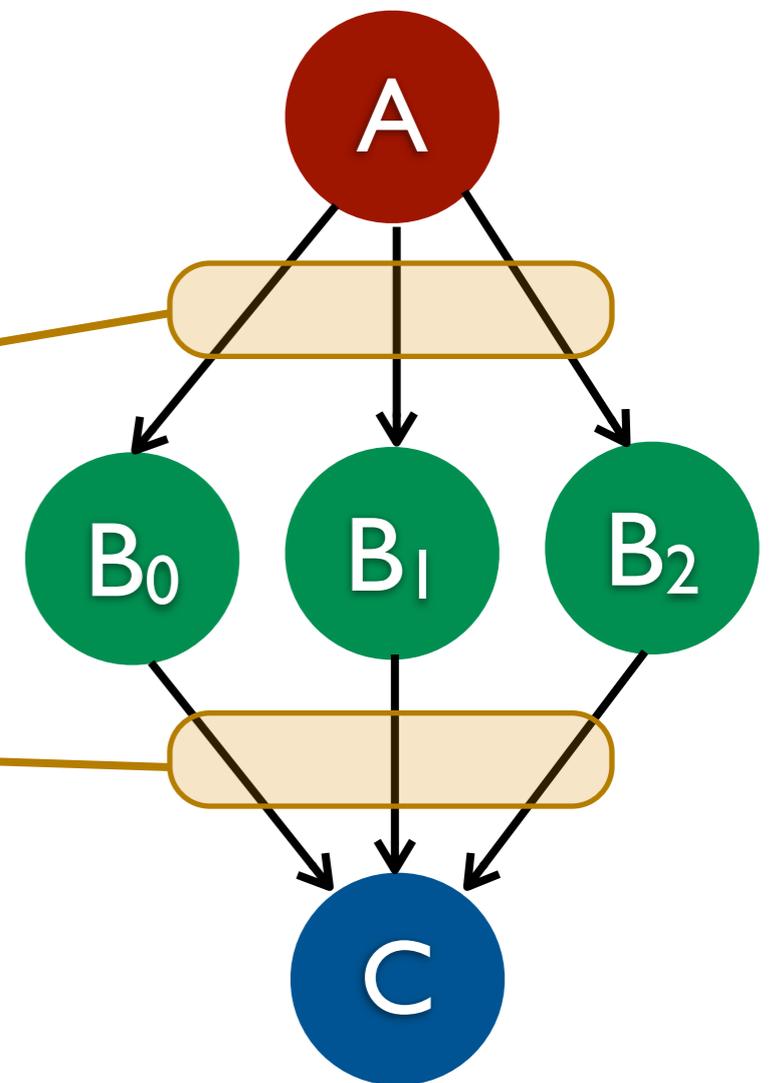
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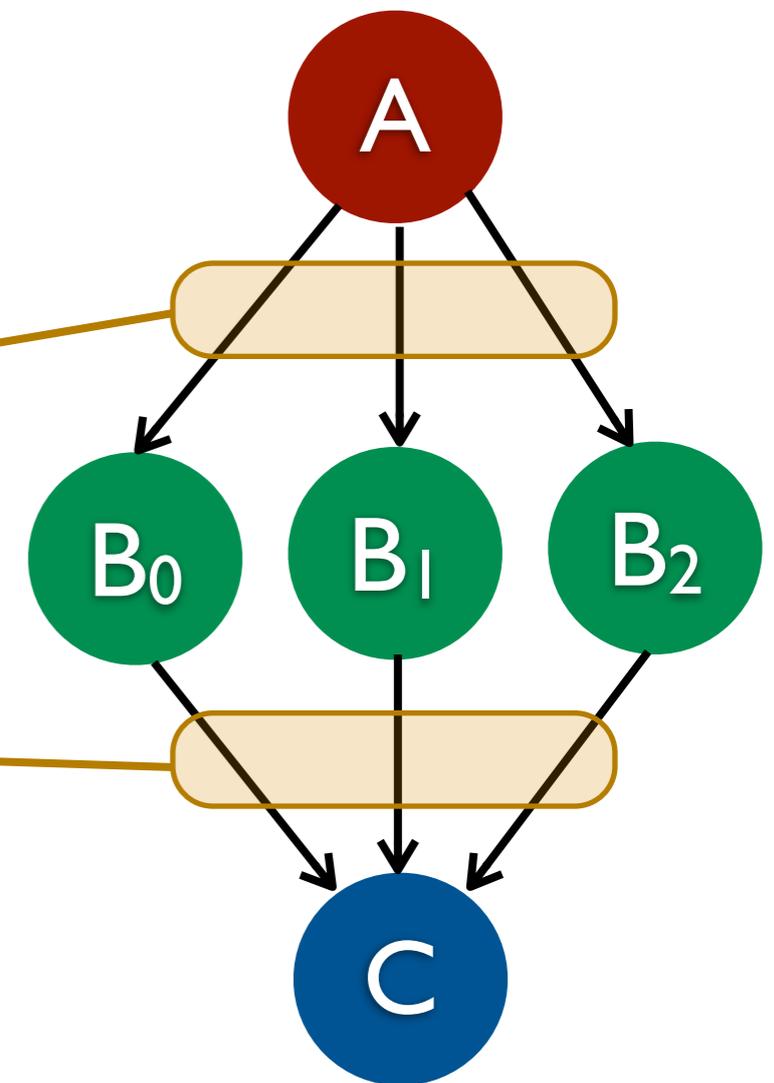
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General enough to express threads,
fork/join, thread libraries, ...

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- **Two Case Studies**
- **Conclusion**

Schedule Analysis

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 - I. Extract schedule summaries from bytecode
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Schedule Analysis

- ▶ Static analysis, works in two phases:
 1. Extract schedule summaries from bytecode
 - ⇒ Task scheduling plus loop-sensitive ordering
 2. Until fixed-point reached:
 - Find tasks that may be created **without ordering**

I: Extract Summaries

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task T1() {  
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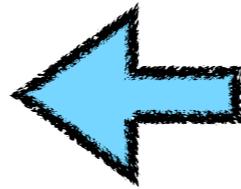
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Schedule Summary

2: Find Unordered Tasks

task T1:

schedules A and B*

with $A \# B$

task T2:

schedules A and B

2: Find Unordered Tasks

- Key insight:
- We look for **unordered-ness**, not **ordered-ness**
- Unordered-ness is **monotonic!**

task T1:

schedules A and B*

with $A \not\# B$

task T2:

schedules A and B

2: Find Unordered Tasks

task T1:

schedules A and B*

with $A \not\ll B$

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schedules A and B

Ordered-ness:

2: Find Unordered Tasks

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Ordered-ness:

for T1: $A \not\ll B$

for T2: \emptyset

2: Find Unordered Tasks

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task T2:
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for T1: ~~$A \not\parallel B$~~
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not monotonic

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Unordered-ness:

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task T2:
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Ordered-ness:

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for T2: \emptyset

not monotonic

Unordered-ness:

for T1: B \parallel B

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task T1:  
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with A ✎ B
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```
task T2:  
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```

Ordered-ness:

```
for T1: A ✎ B  
for T2: ∅
```

not monotonic

Unordered-ness:

```
for T1: B || B  
for T2: A || B
```

2: Find Unordered Tasks

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task T1:  
  schedules A and B*  
with A ≠ B
```

```
task T2:  
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```

Ordered-ness:

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for T1: A ≠ B  
for T2: ∅
```

not monotonic

Unordered-ness:

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for T1: B ∥ B  
for T2: A ∥ B
```

monotonic

Summary Schedule Analysis

- Static bytecode analysis
- Computes relation:
`maybeParallel(task1, task2)`
- If `!maybeParallel(task1, task2)` then `task1` and `task2` are guaranteed to be ordered

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- Motivation
- Task Model
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- **Two Case Studies**
 - **Sequentially Consistent Java**
 - **Dynamic Fractional Permissions**
- **Conclusion**

Sequential Consistency

- Easy-to-understand memory model
- Conceptually:
 - All memory accesses are visible immediately
 - All tasks agree on same legal sequential history of memory events
 - No instruction re-ordering

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- Conceptually:
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**Inefficient without
optimizations!**

SC Example

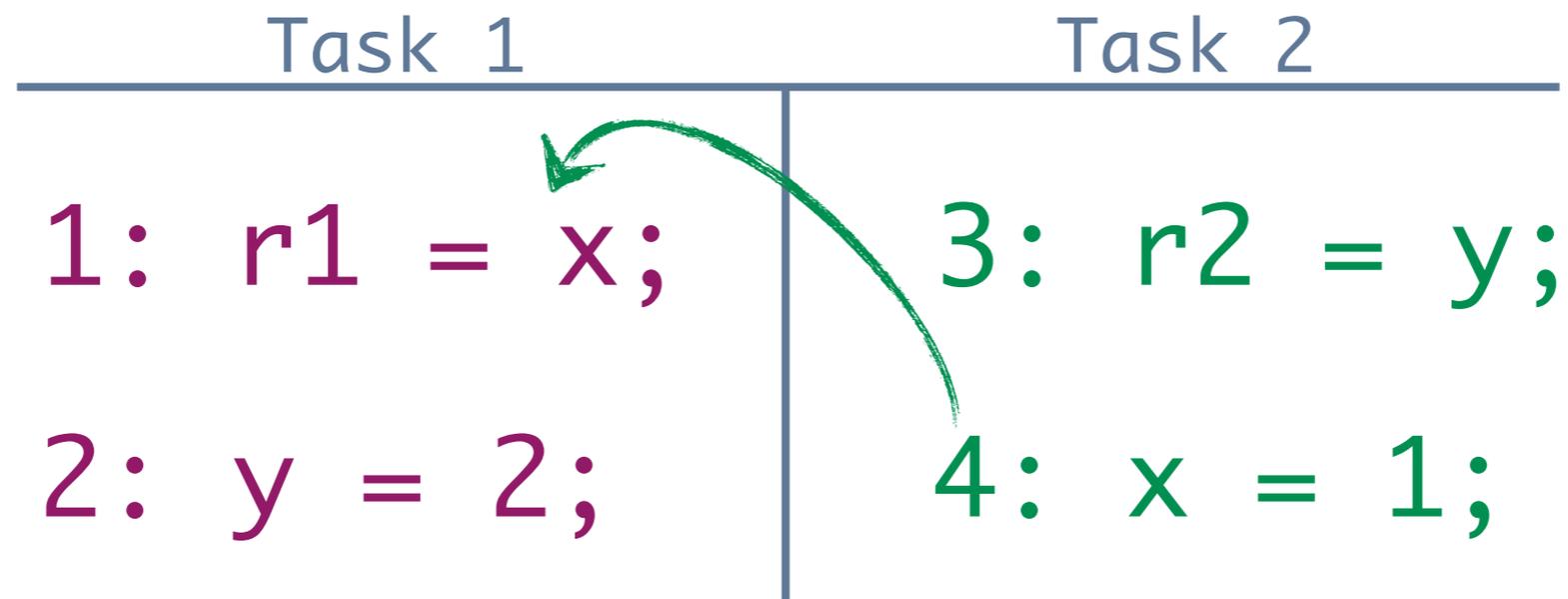
Initially, $x == y == 0$

Task 1	Task 2
1: $r1 = x;$	3: $r2 = y;$
2: $y = 2;$	4: $x = 1;$

Is $r1 == 1$ AND $r2 == 2$ possible?

SC Example

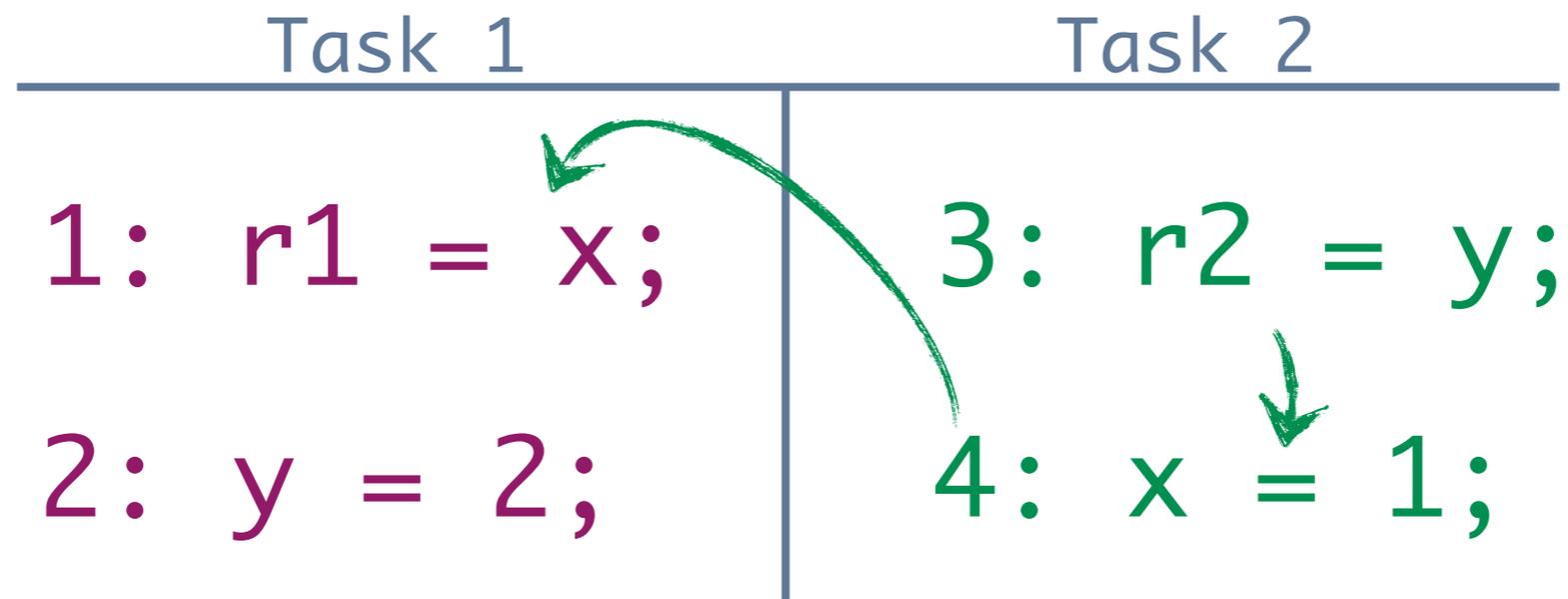
Initially, $x == y == 0$



Is $r1 == 1$ AND $r2 == 2$ possible?

SC Example

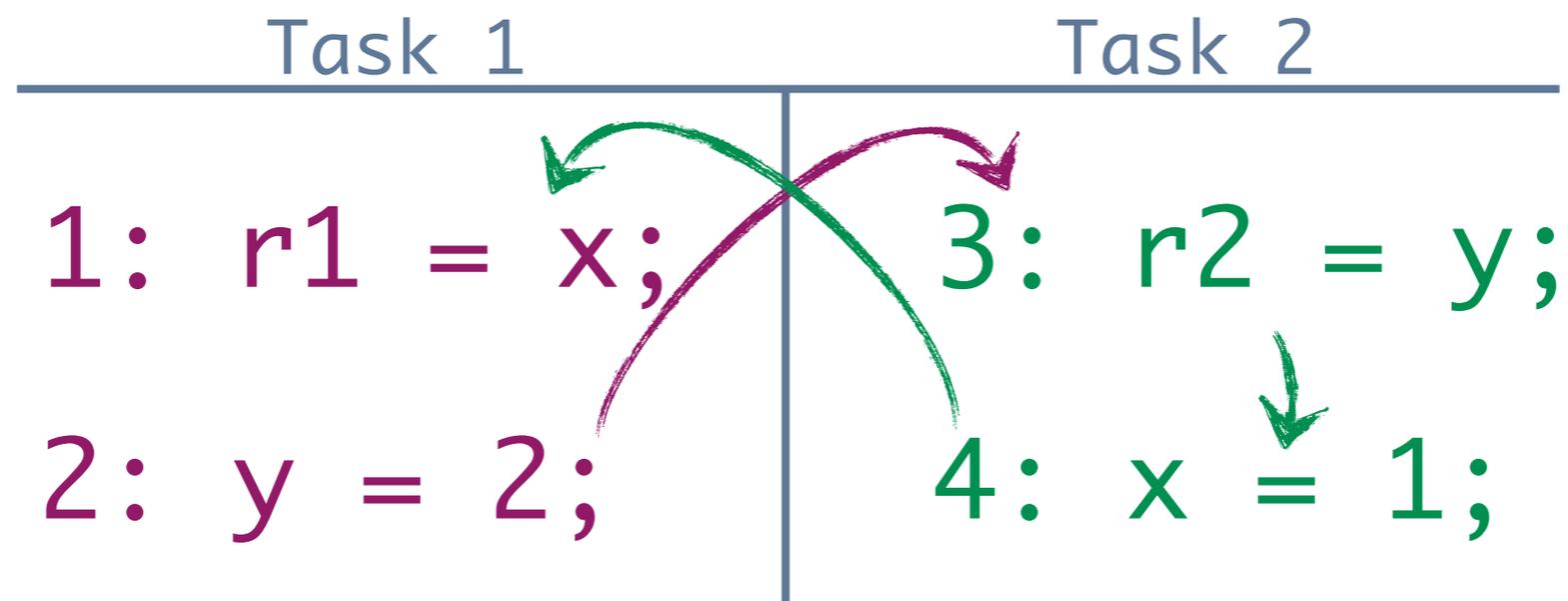
Initially, $x == y == 0$



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SC Example

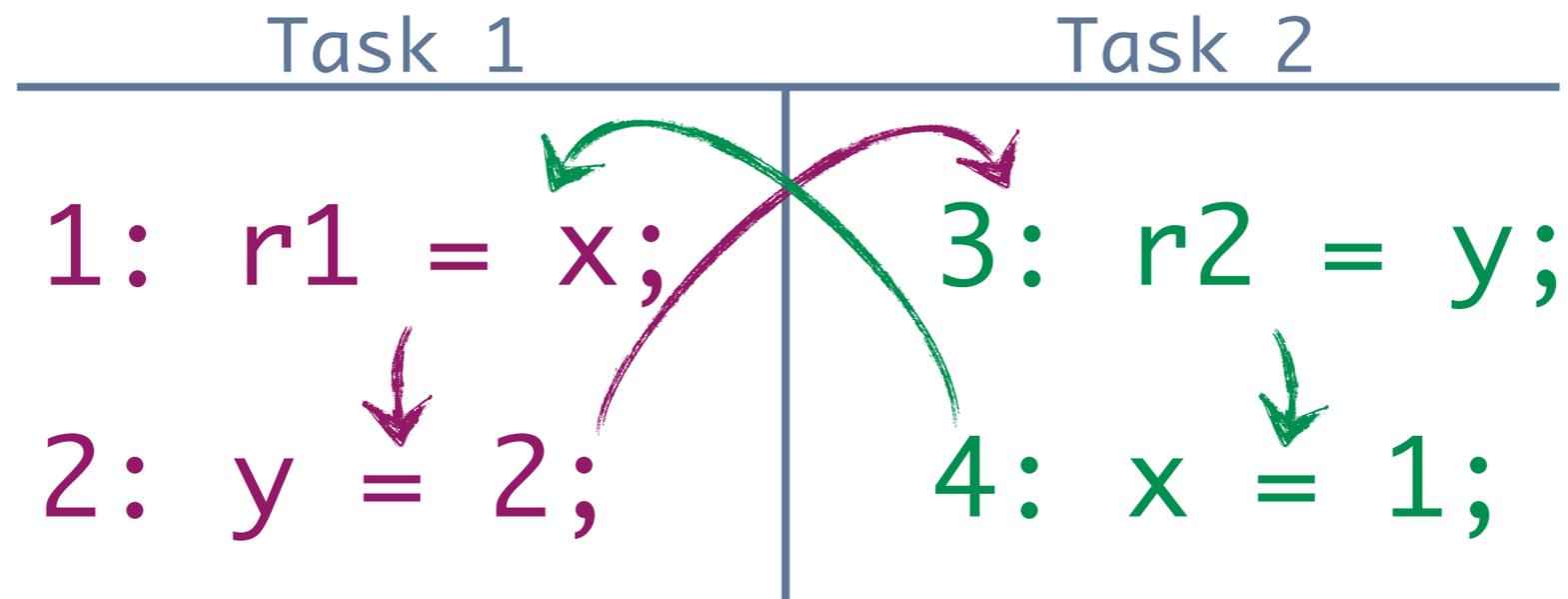
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SC Example

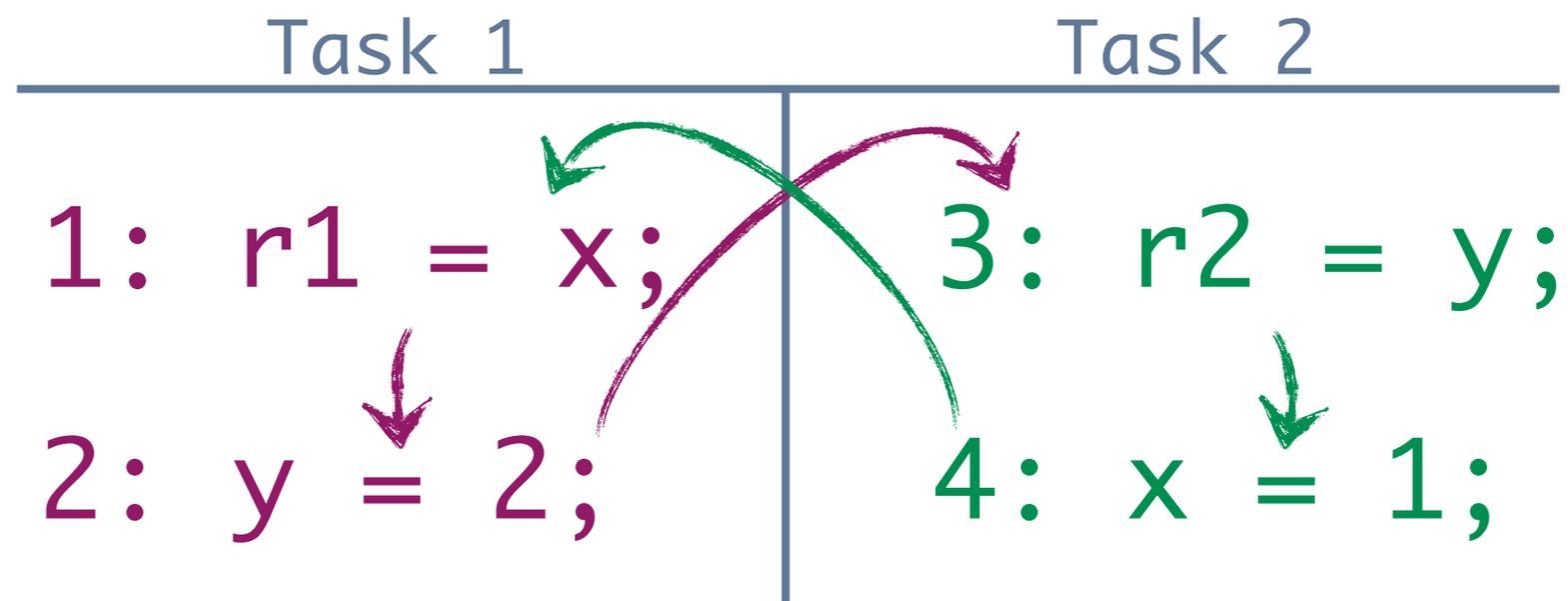
Initially, $x == y == 0$



Is $r1 == 1$ AND $r2 == 2$ possible?

SC Example

Initially, $x == y == 0$



Is $r1 == 1$ AND $r2 == 2$ possible?

No, if “sequentially consistent”

SC Example

Initially, $x == y == 0$

Task 1	Task 2
2: $y = 2;$	4: $x = 1;$
1: $r1 = x;$	3: $r2 = y;$

Is $r1 == 1$ AND $r2 == 2$ possible?

**Yes, if the compiler reorders
1,2 and/or 3,4**

Sequentially Consistent Java

Sequentially Consistent Java

- Simple model:
 - Guard every memory access with **barriers** (fields and array elements)

Sequentially Consistent Java

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- Drawbacks:
 - **Barriers** introduce overhead
 - Prevents many standard optimizations

Sequentially Consistent Java

- Simple model:
 - Guard every memory access with **barriers** (fields and array elements)
- Drawbacks:
 - **Barriers** introduce overhead
 - Prevents many standard optimizations
- Optimize to re-gain performance:
 - Remove **barriers** where not needed
 - **Different** objects \vee **ordered** tasks

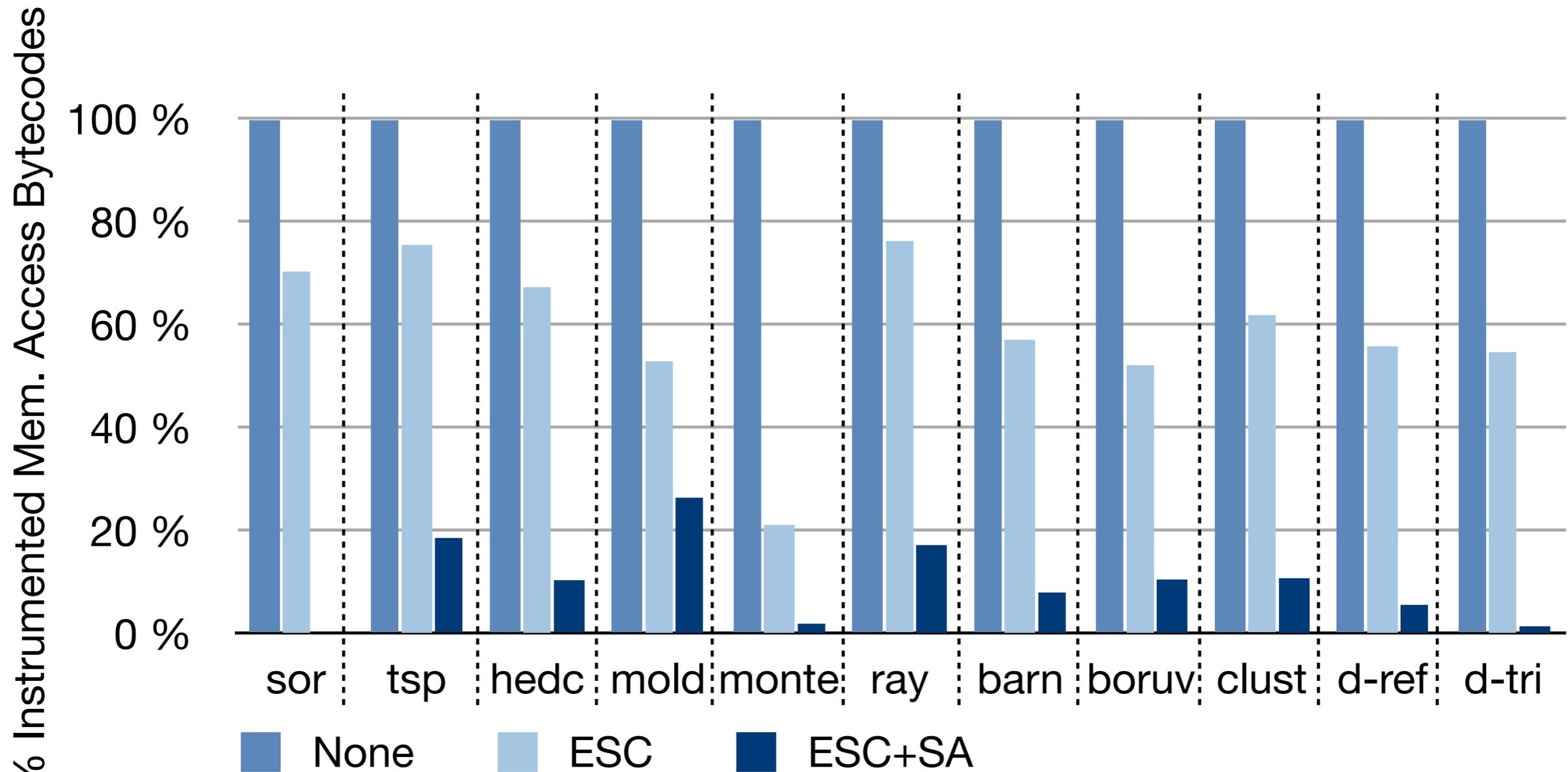
Evaluation Setup

- Intel Core 2 Duo, 2.8 GHz, 4Gb RAM
 - ⇒ 2 Java Threads
- Java 1.6.0 (Mac)
- Benchmarks
 - **Java Grande**: numeric apps
 - **Erco Benchmarks**: OO-style parallelism
 - **Lonestar**: larger applications, irregular behavior

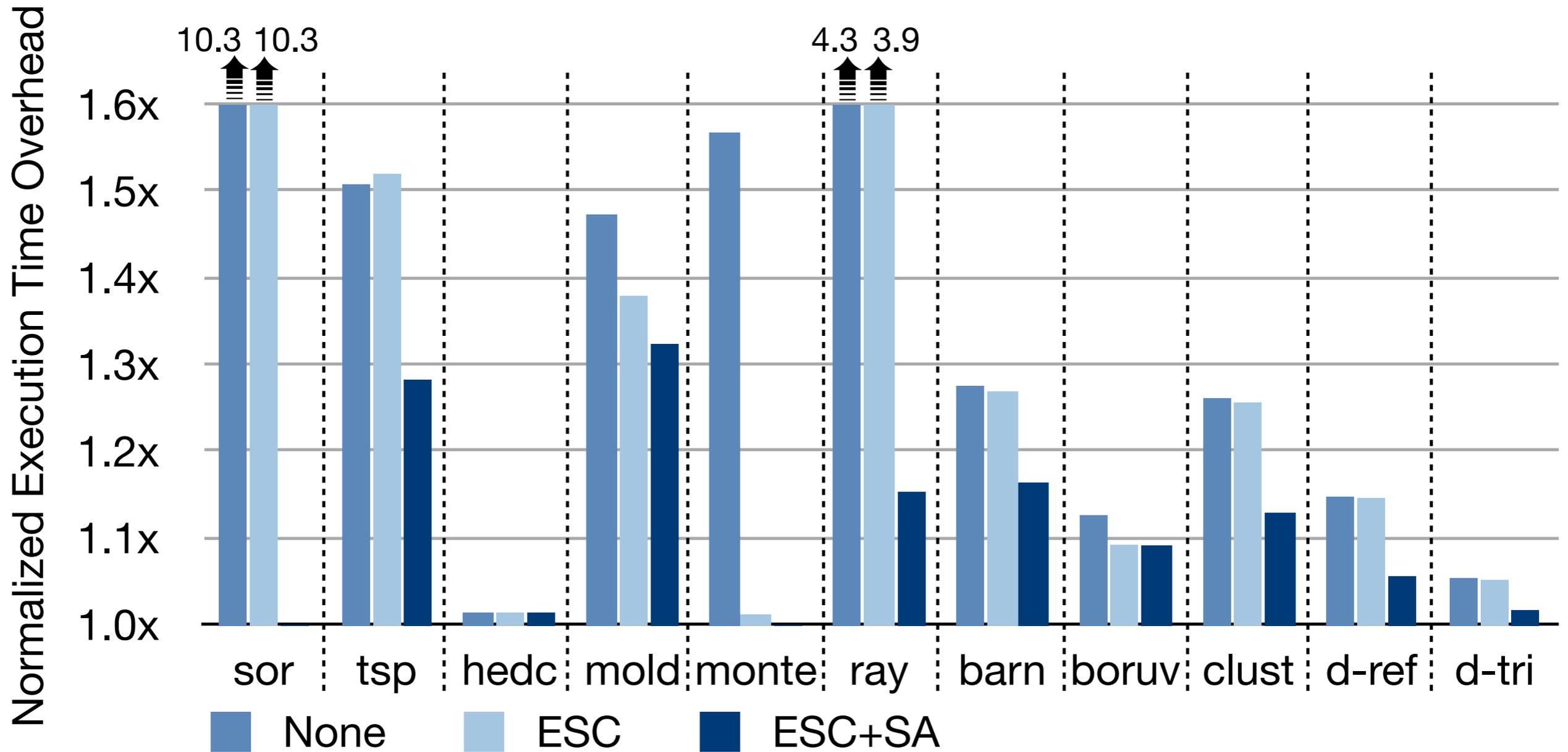
Configurations

- Relaxed memory model, programmer-provided SC (Baseline)
- SC, no optimizations (None)
- SC, escape analysis (ESC)
- SC, schedule analysis + escape analysis (SA+ESC)

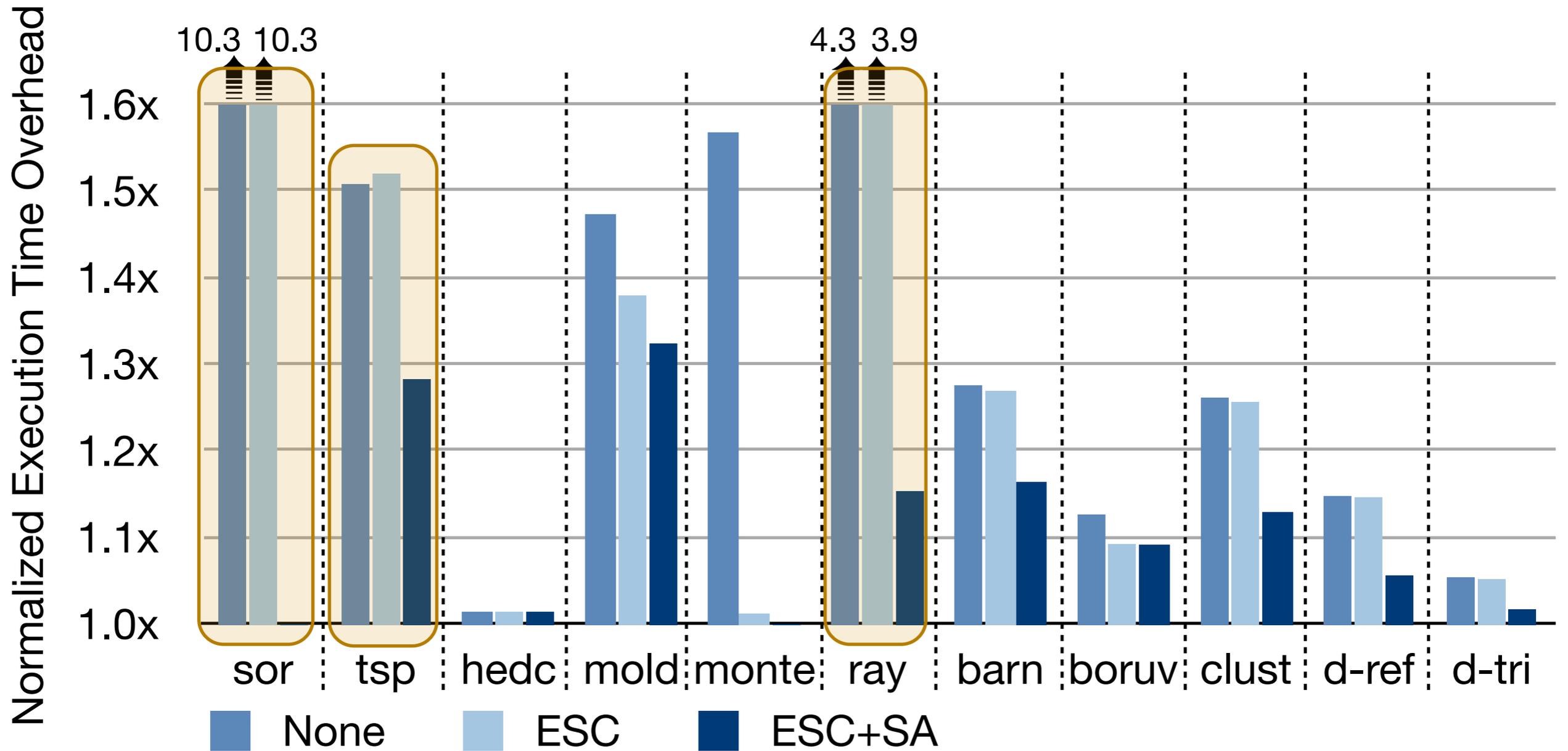
Instrumentation Overhead



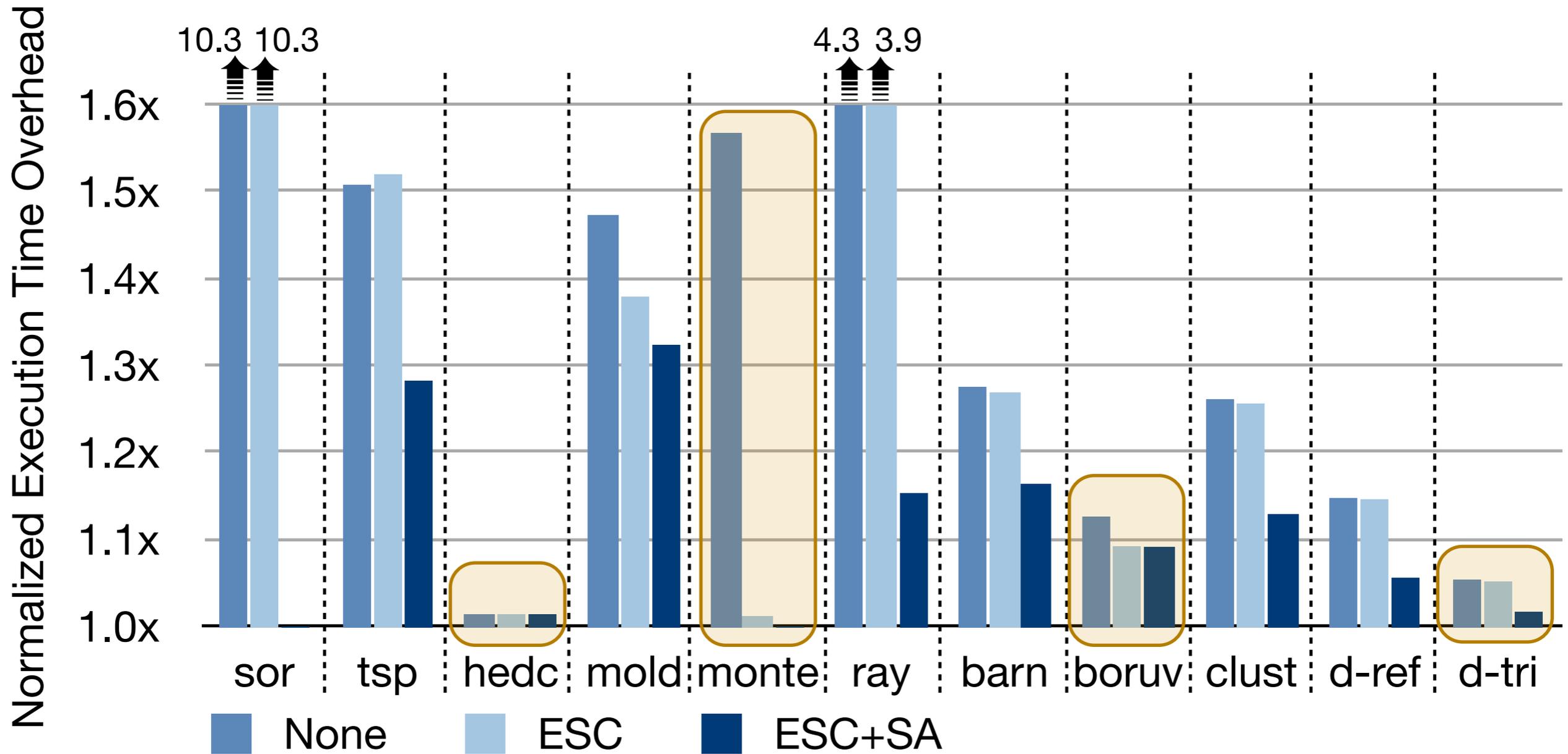
Execution Time



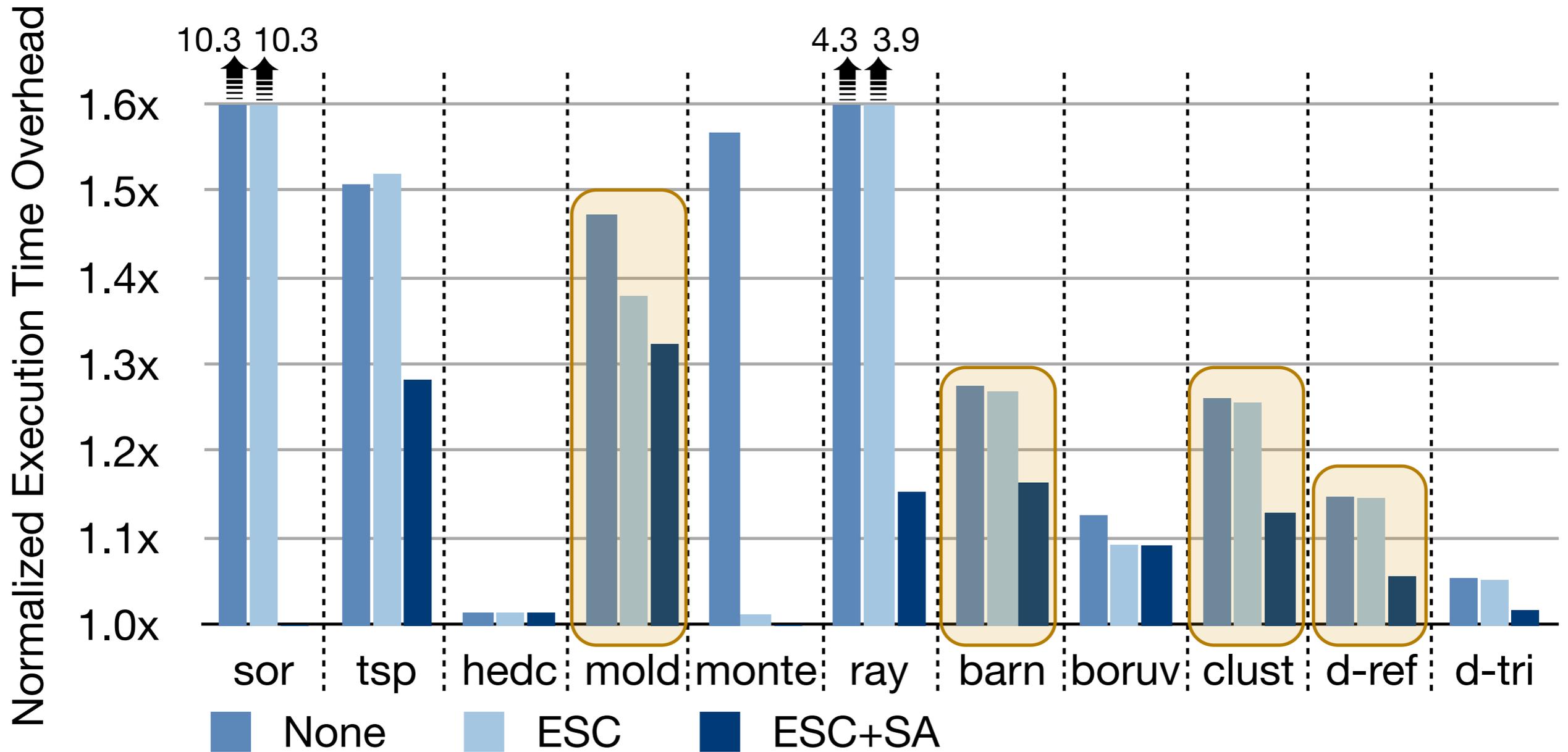
Execution Time



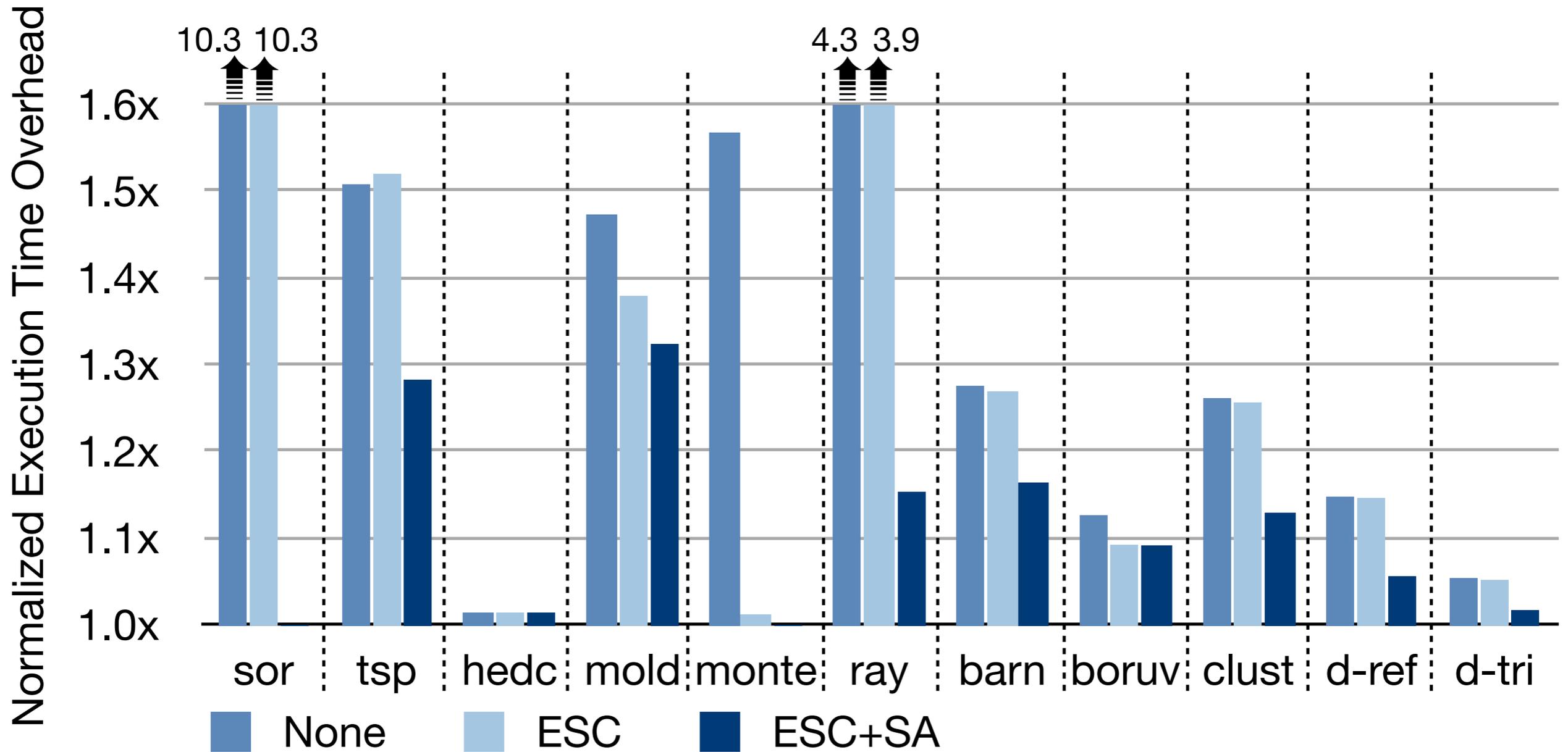
Execution Time



Execution Time



Execution Time



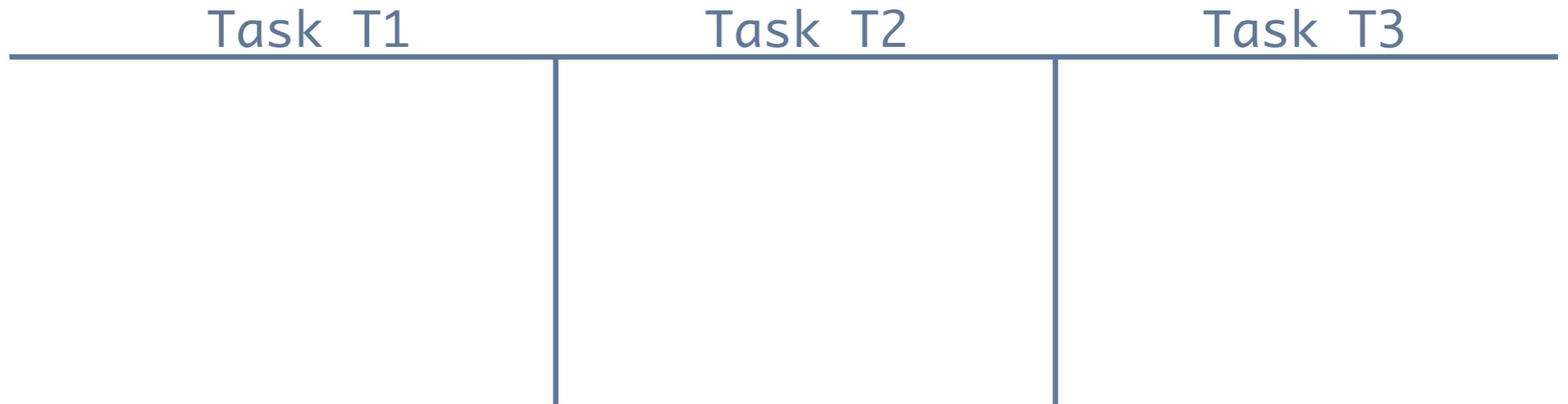
Outline

- Motivation
- Task Model
- Schedule Analysis
- Two Case Studies
 - Sequentially Consistent Java
 - **Dynamic Fractional Permissions**
- **Conclusion**

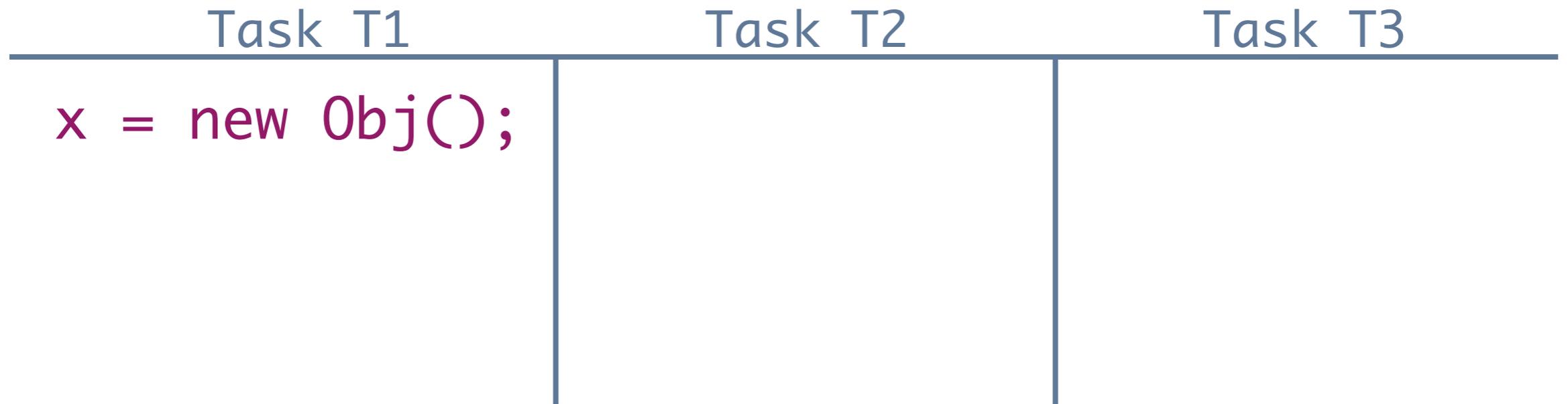
Dynamic Fractional Permissions

- Dynamic version of static data-race detection framework [Boyland 2003]
- Programmer manages access permissions:
 - Every object o has associated access control list
 - Task $T \in \text{ACL}(o) \Rightarrow$ read access
 - Task T **only** task in $\text{ACL}(o) \Rightarrow$ write access
- Compiler inserts permission checks

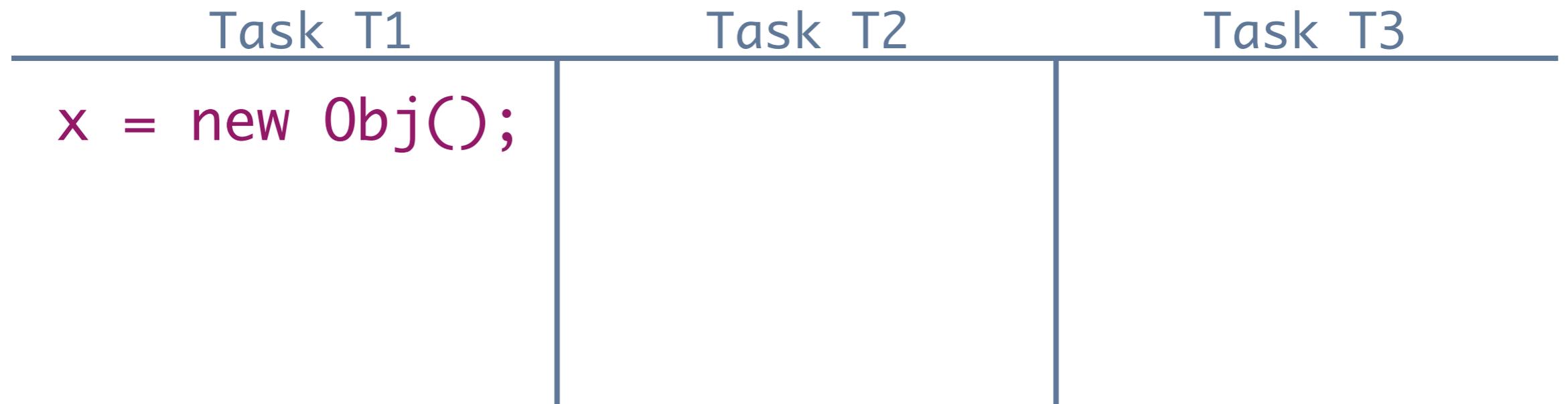
Permission Operations



Permission Operations

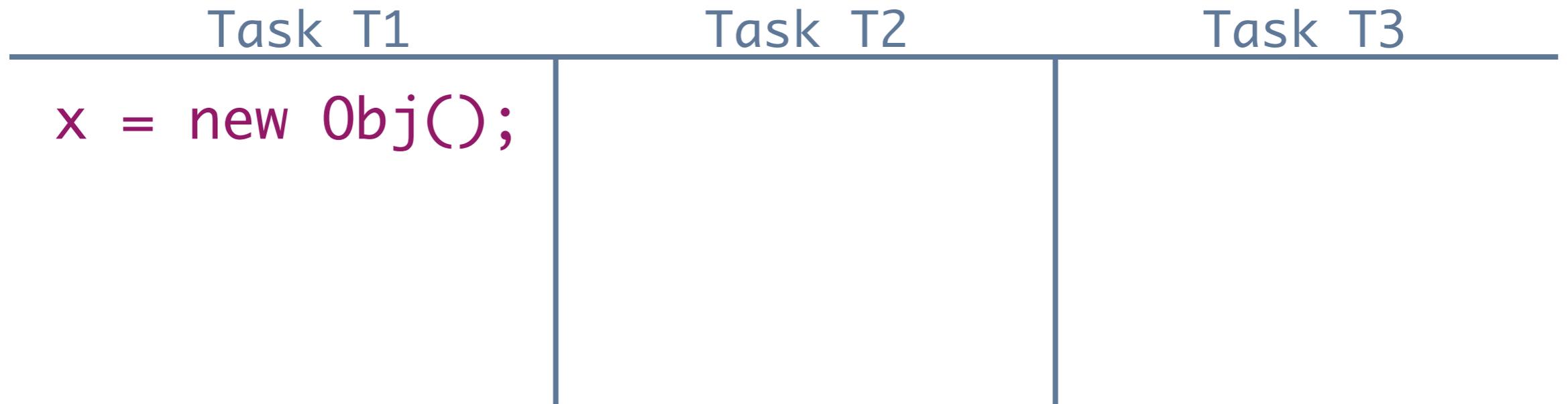


Permission Operations



ACL(x): {T1}

Permission Operations



ACL(x): {T1}

Permissions:

T1

T2

T3

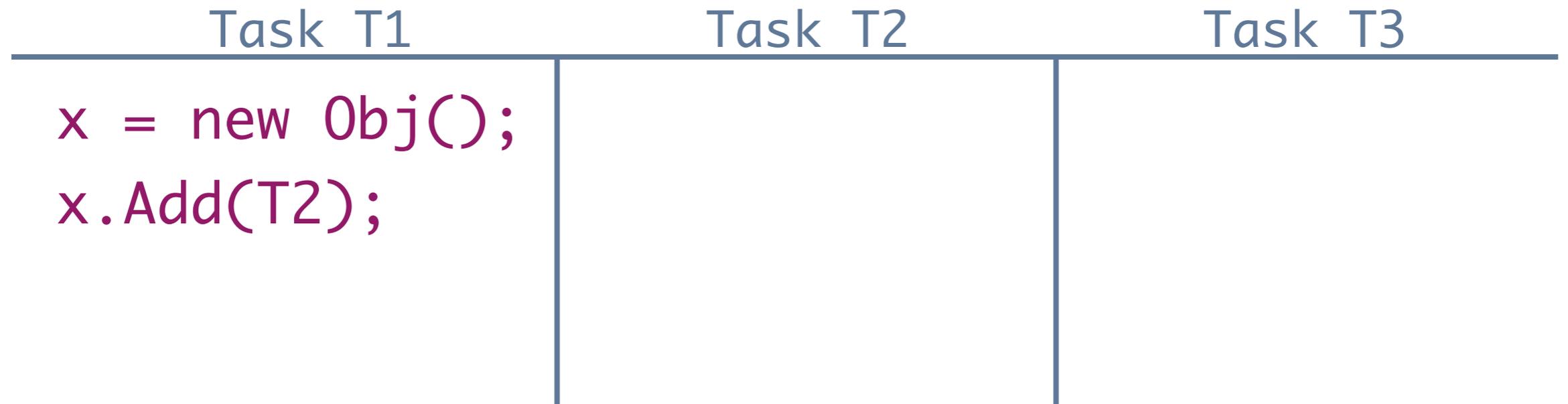
Can read x:



Can write x:

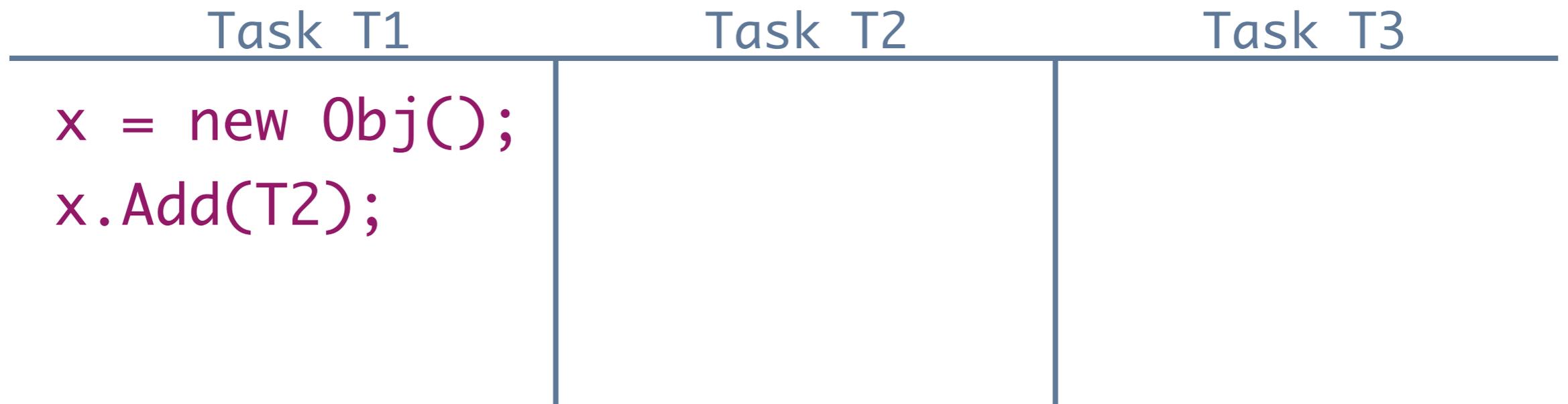


Permission Operations



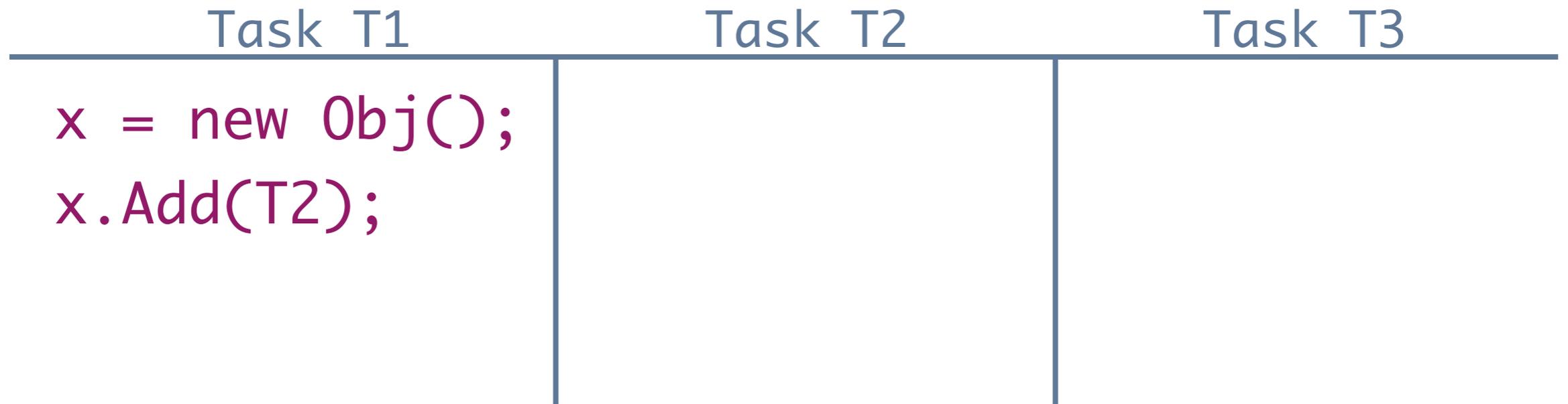
ACL(x): {T1}

Permission Operations



ACL(x): {T1, T2}

Permission Operations



ACL(x): {T1, T2}

Permissions:

T1

T2

T3

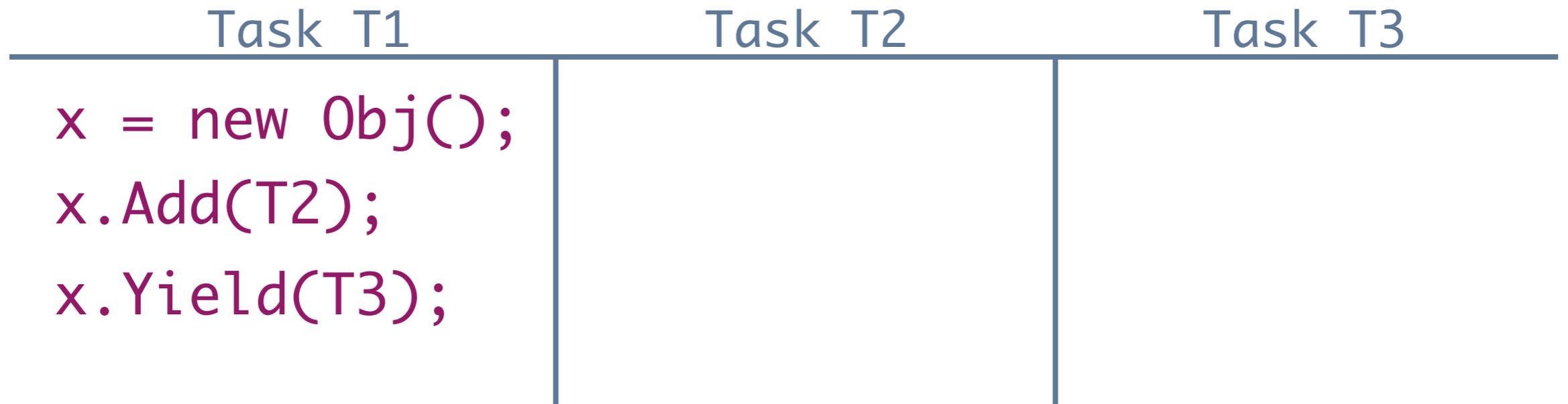
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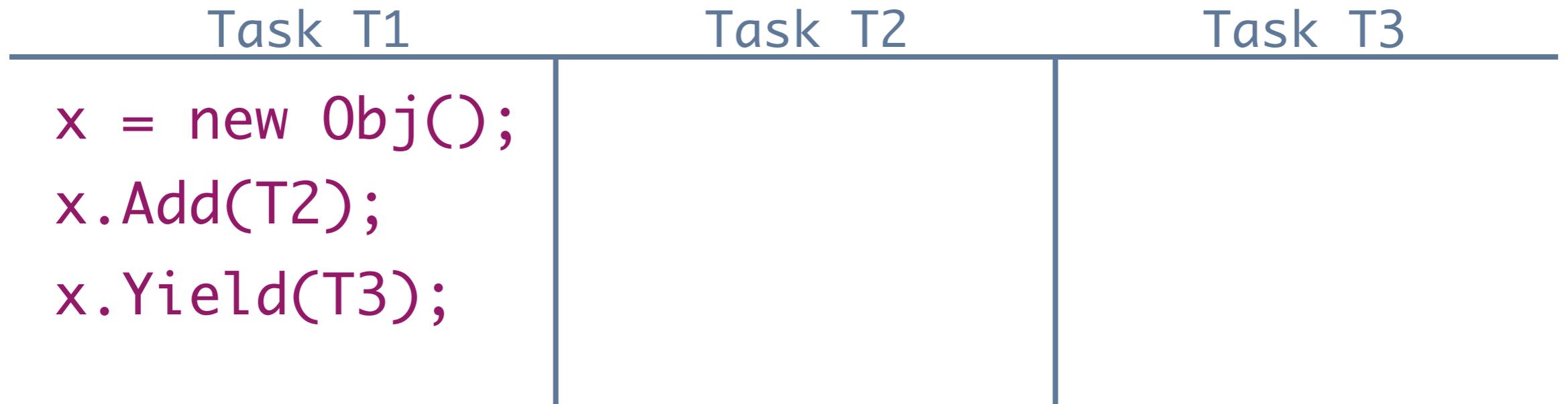


Permission Operations



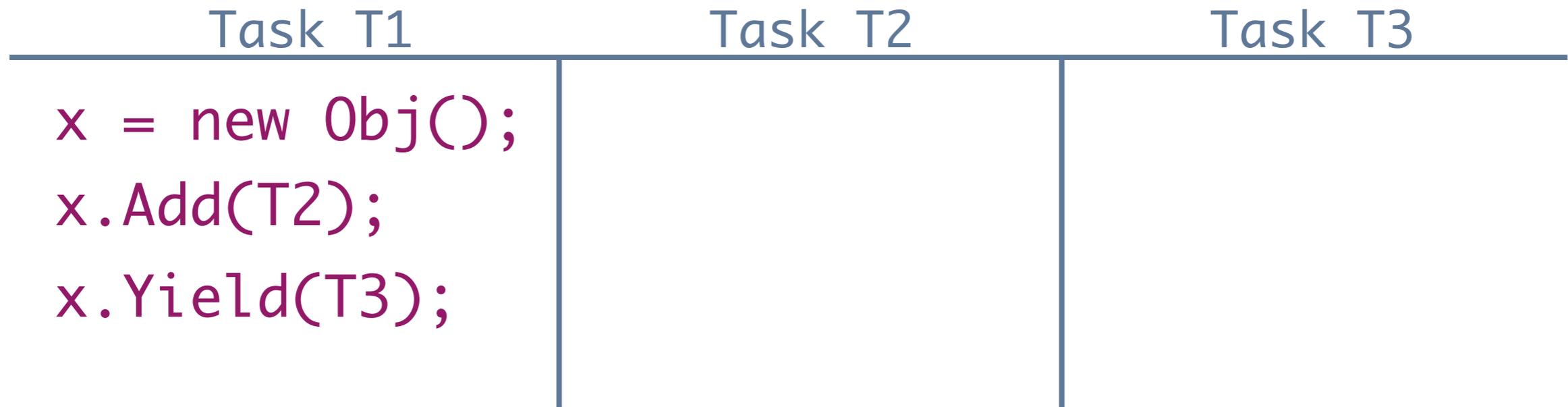
ACL(x): {T1, T2}

Permission Operations



ACL(x): {T3, T2}

Permission Operations



ACL(x): {T3, T2}

Permissions:

T1

T2

T3

Can read x:



Can write x:



Permission Operations

Task T1	Task T2	Task T3
<pre>x = new Obj(); x.Add(T2); x.Yield(T3);</pre>	<pre>x.Yield(T3);</pre>	

ACL(x): {T3, T2}

Permission Operations

Task T1	Task T2	Task T3
<pre>x = new Obj(); x.Add(T2); x.Yield(T3);</pre>	<pre>x.Yield(T3);</pre>	

ACL(x): {T3}

Permission Operations

Task T1	Task T2	Task T3
<pre>x = new Obj(); x.Add(T2); x.Yield(T3);</pre>	<pre>x.Yield(T3);</pre>	

ACL(x): {T3}

Permissions:

T1

T2

T3

Can read x:



Can write x:



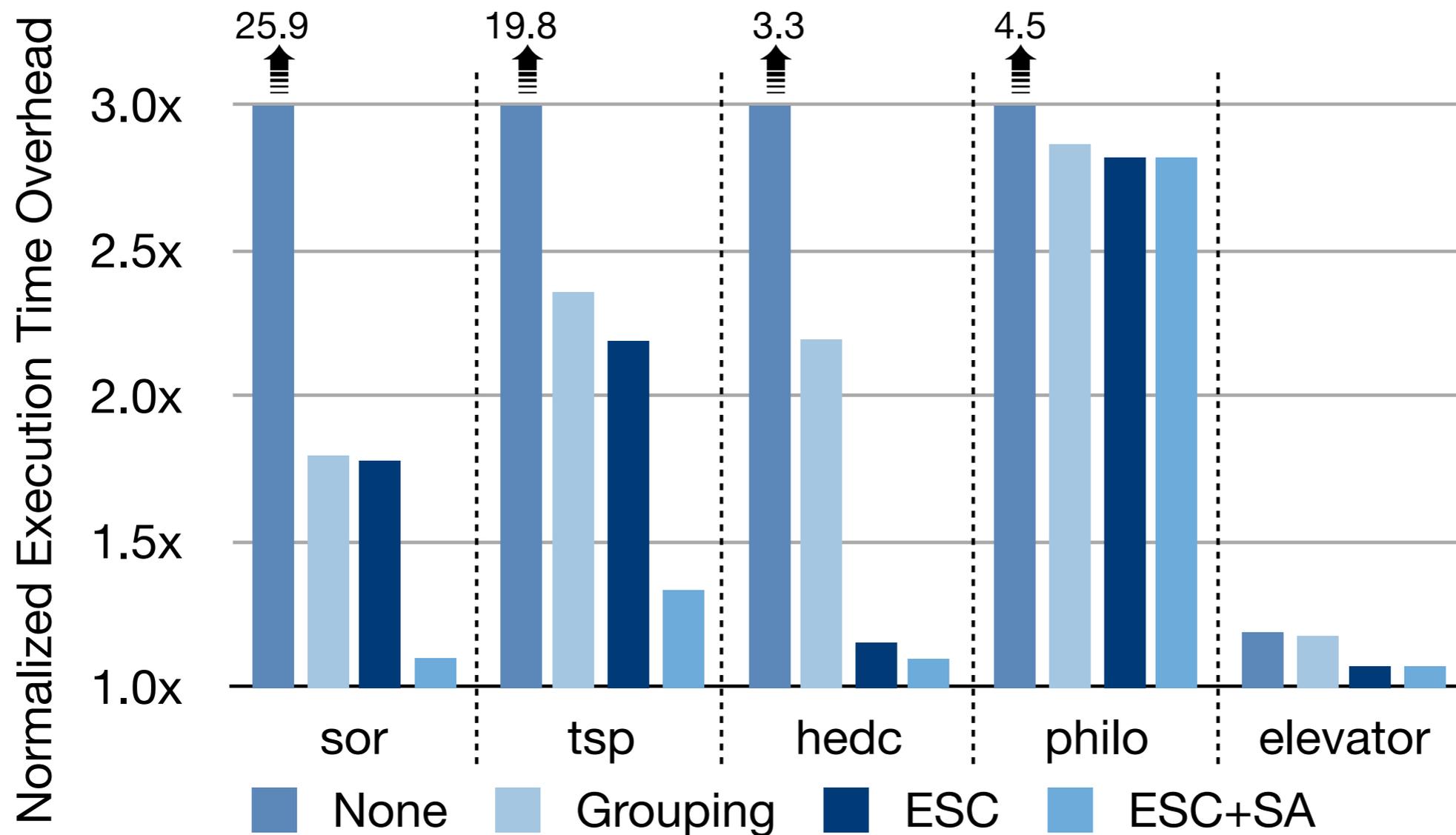
Optimizations

- Group redundant permission checks (method-local)
- Remove `new`, `Add`, and `Yield` operations for task-local objects
- Reduce number of inserted permission checks

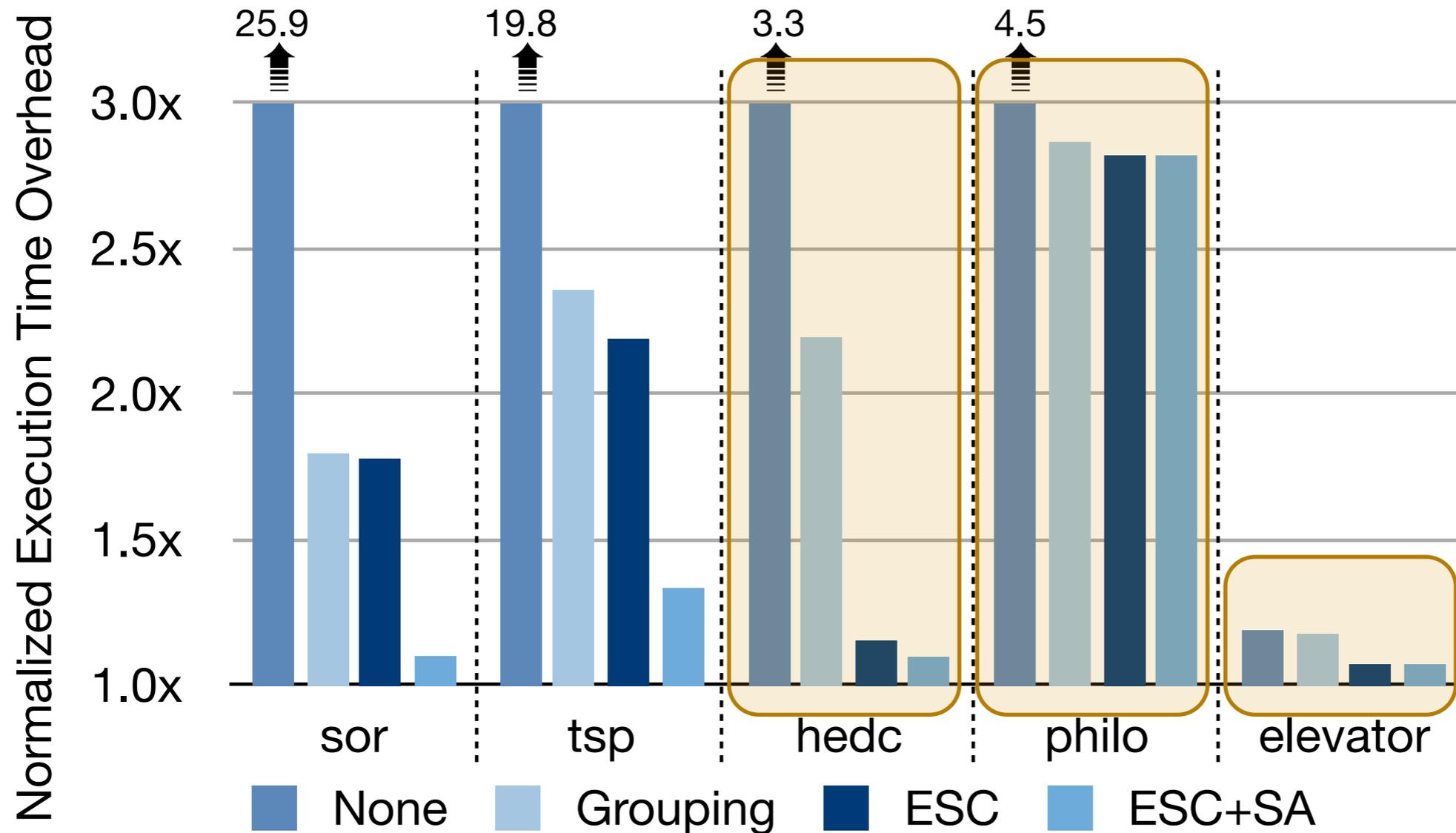
Configurations

- No permission system (**Baseline**)
- No optimizations, permission checks on all accesses (**None**)
- Grouping of redundant permission checks (**Group**)
- Escape analysis (**ESC**)
- Schedule analysis + escape analysis (**SA+ESC**)

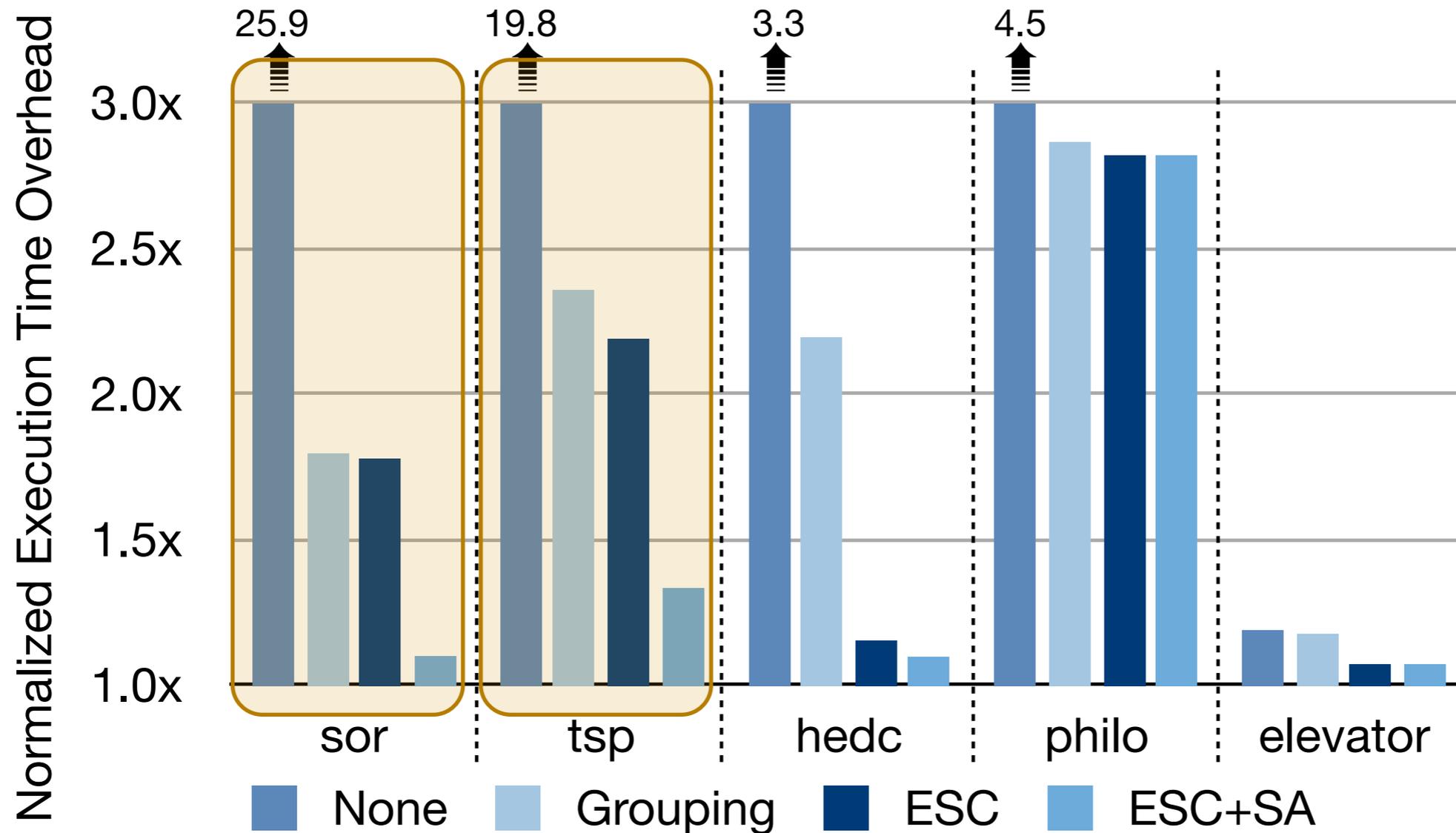
Execution Time



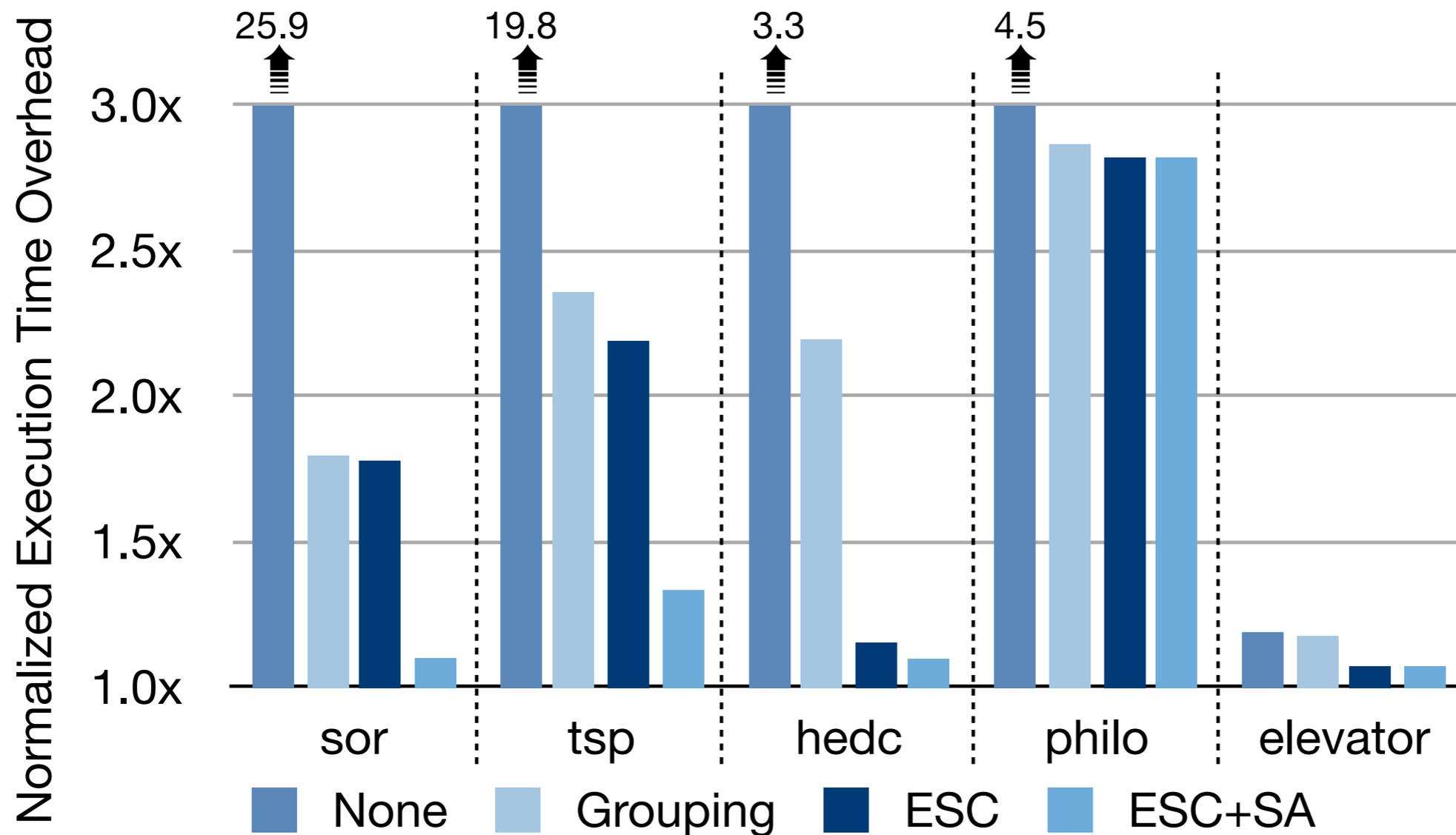
Execution Time



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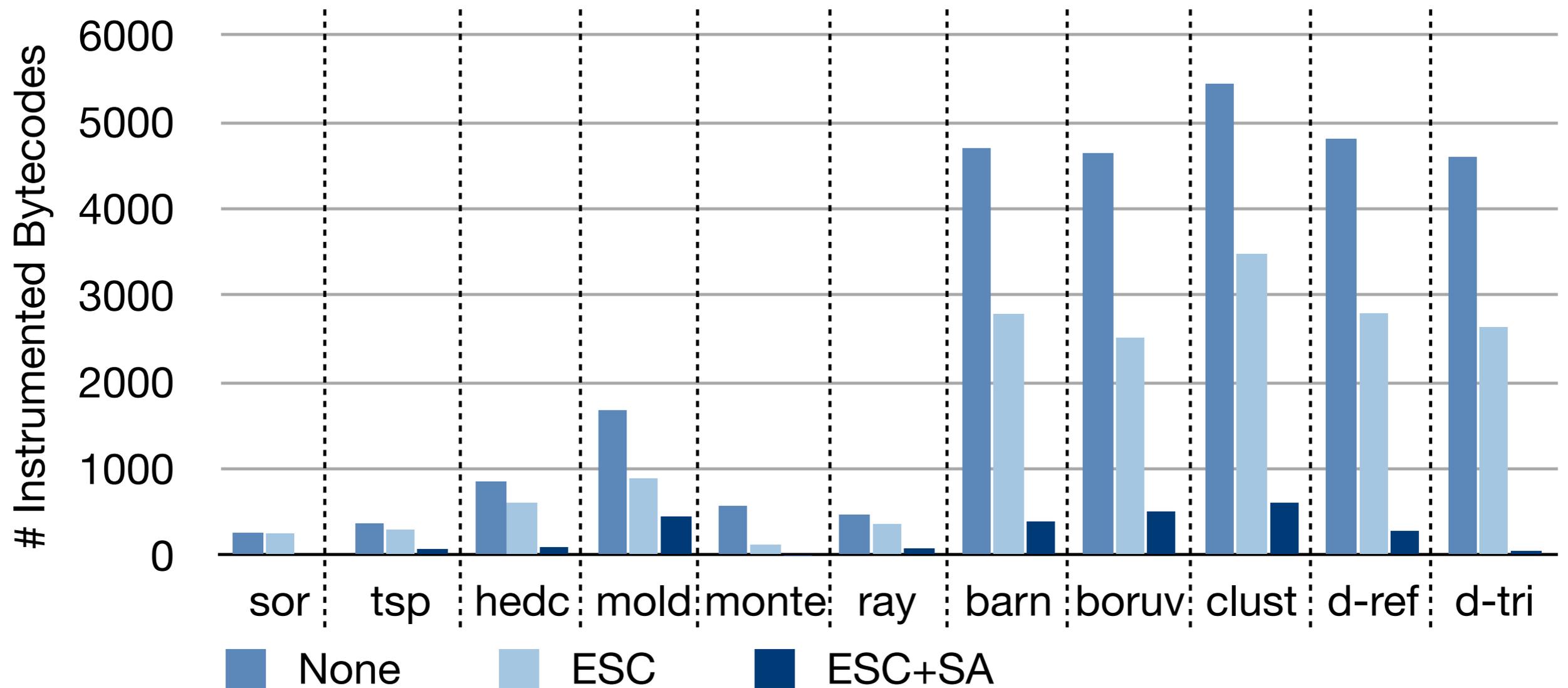
Conclusion

- Compilers for shared-memory parallel programs can exploit **task-order information**
- **Schedule analysis:**
 - can extract task-order information from **real-world** programs
 - provides basis for **effective** optimizations

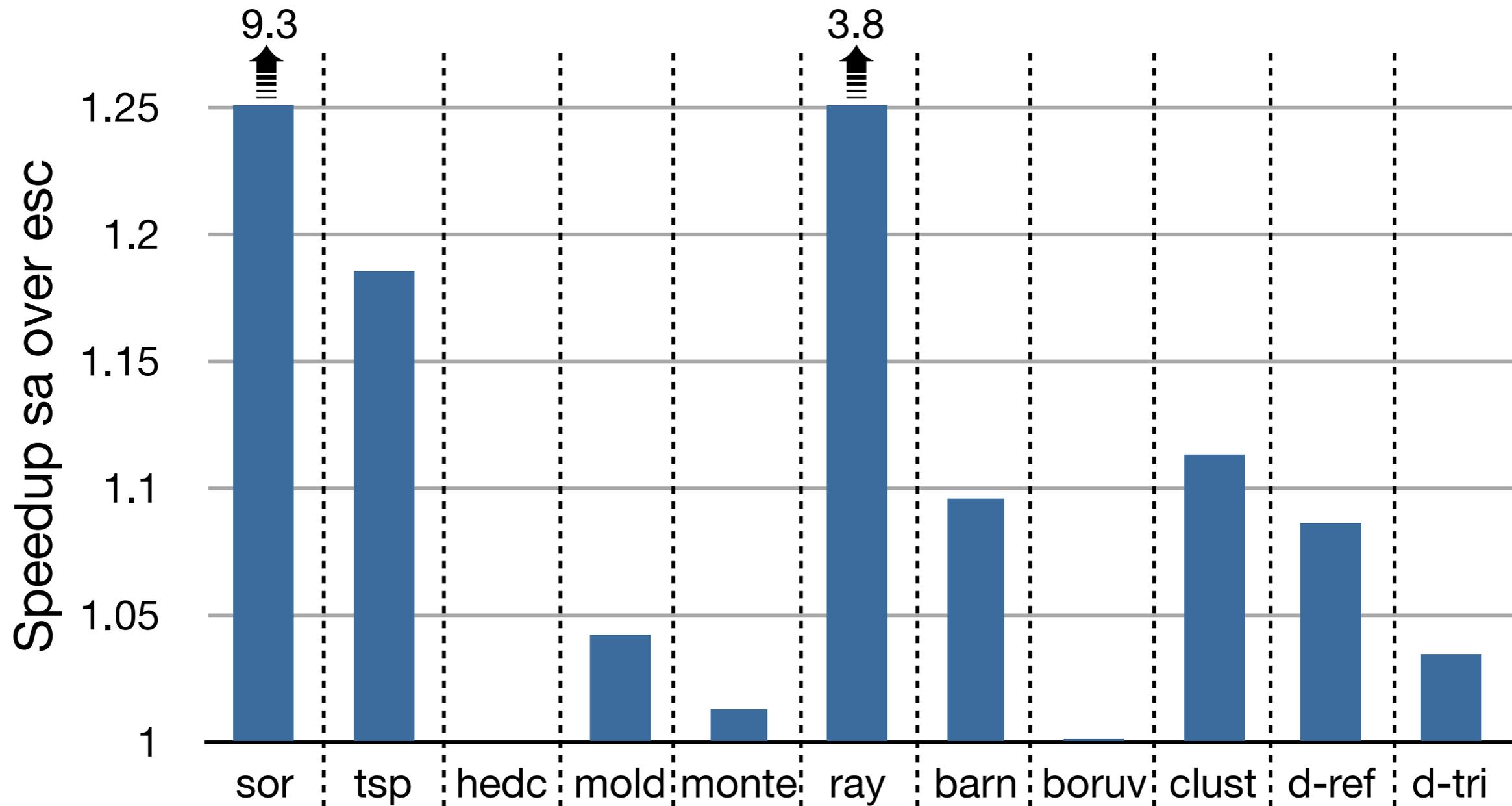
Implementation

- Bytecode-to-bytecode translation with `getVolatile()` and `putVolatile()` intrinsics
- Analyzes bytecode in SSA form
- Wala framework for analysis,
- Javassist for code generation

Instrumentation Overhead



Speedup SA+ESC over ESC



Related Work

- **Compiler techniques for high performance sequentially consistent java programs.** Z.
Sura et al, PPOPP'05
- **A case for an SC-preserving compiler.** D.
Marino et al, PLDI'11
- **Efficient sequential consistency using conditional fences.** C. Lin, V Nagarajan, R. Gupta, PACT'10
- **BulkCompiler: high-performance sequential consistency through cooperative compiler and hardware support.** W. Ahn et al, MICRO'09
- **MHP Analysis.** (Agarwal et al)

Ordering with Threads

`/*A*/`

```
Thread[] ts = new Thread[3];  
for(int i=0; i<3; i++) {  
    ts[i] = new MyThread(/*B*/);  
    ts[i].start();  
}  
for(int i=0; i<3; i++)  
    ts[i].join();
```

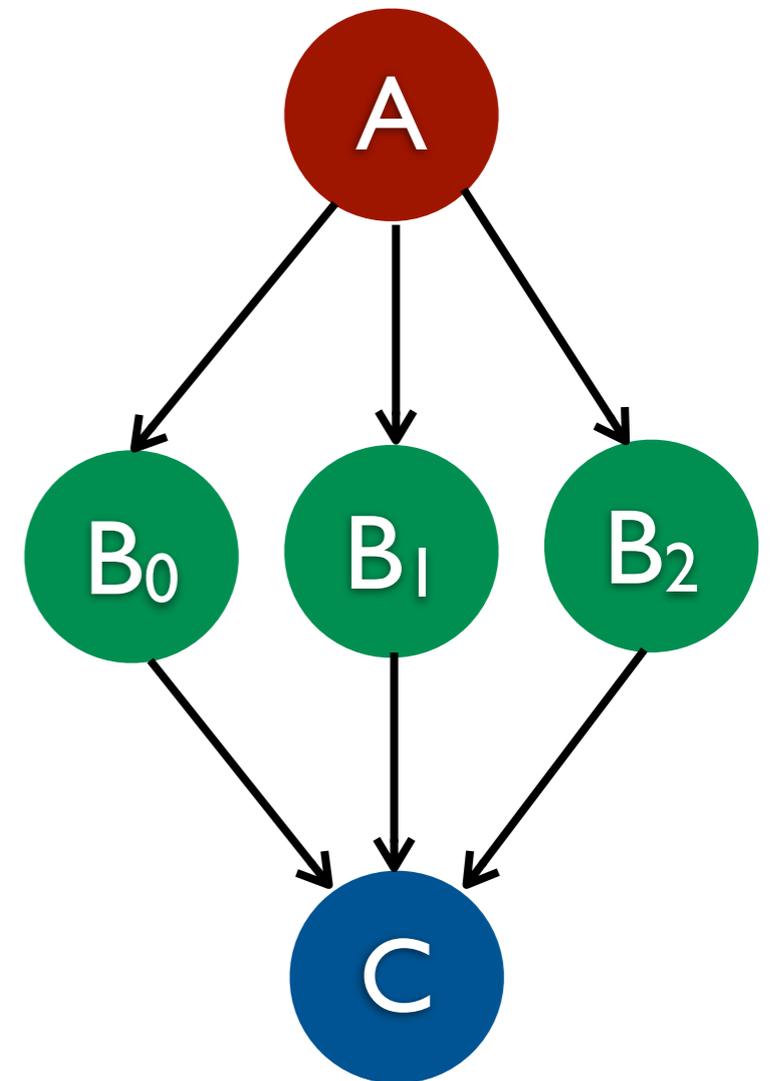
`/*C*/`

Ordering with Threads

```
/*A*/
```

```
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for(int i=0; i<3; i++) {  
    ts[i] = new MyThread(/*B*/);  
    ts[i].start();  
}  
for(int i=0; i<3; i++)  
    ts[i].join();
```

```
/*C*/
```



Ordering in OpenMP

```
/*A*/
```

```
//#omp parallel for
```

```
for(int i=0; i<3; i++) {
```

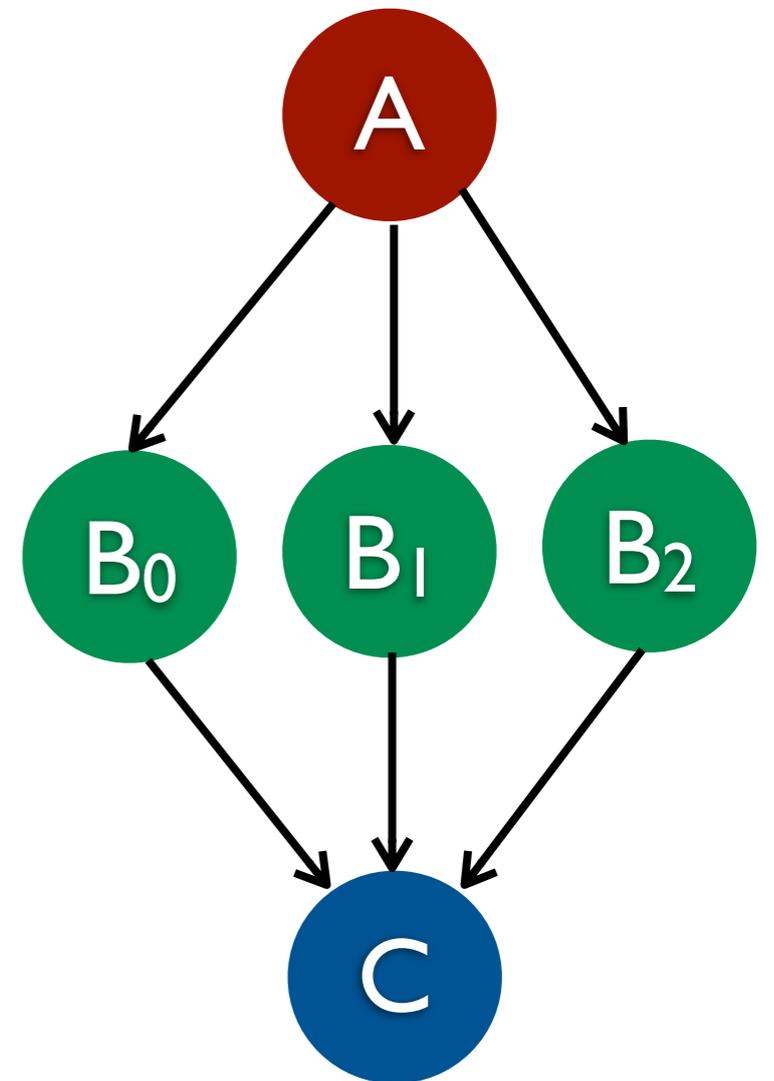
```
    /*B*/
```

```
}
```

```
/*C*/
```

Ordering in OpenMP

```
/*A*/  
  
//#omp parallel for  
for(int i=0; i<3; i++) {  
    /*B*/  
}  
  
/*C*/
```



Permission Operations

Permission Operations

```
/*permission management*/
```

Permission Operations

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```
@T1: o = new C()      ⇒ ACL(o) = {T1}
```

Permission Operations

```
/*permission management*/
```

```
@T1: o = new C()           ⇒ ACL(o) = {T1}
```

```
@T1: o.Add(T2)            ⇒ ACL(o) ∪ {T2}
```

Permission Operations

*/*permission management*/*

@T1: $o = \text{new } C()$ $\Rightarrow \text{ACL}(o) = \{T1\}$

@T1: $o.\text{Add}(T2)$ $\Rightarrow \text{ACL}(o) \cup \{T2\}$

@T1: $o.\text{Yield}(T2)$ $\Rightarrow [T1 \mapsto T2]\text{ACL}(o)$

Permission Operations

*/*permission management*/*

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*/*inserted by compiler*/*

Permission Operations

*/*permission management*/*

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*/*inserted by compiler*/*

@T1: $o.\text{CheckRead}()$ $\Rightarrow \text{true}$ iff $T1 \in \text{ACL}(o)$

Permission Operations

*/*permission management*/*

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*/*inserted by compiler*/*

@T1: $o.\text{CheckRead}()$ $\Rightarrow \text{true}$ iff $T1 \in \text{ACL}(o)$

@T1: $o.\text{CheckWrite}()$ $\Rightarrow \text{true}$ iff $\text{ACL}(o) == \{T1\}$